

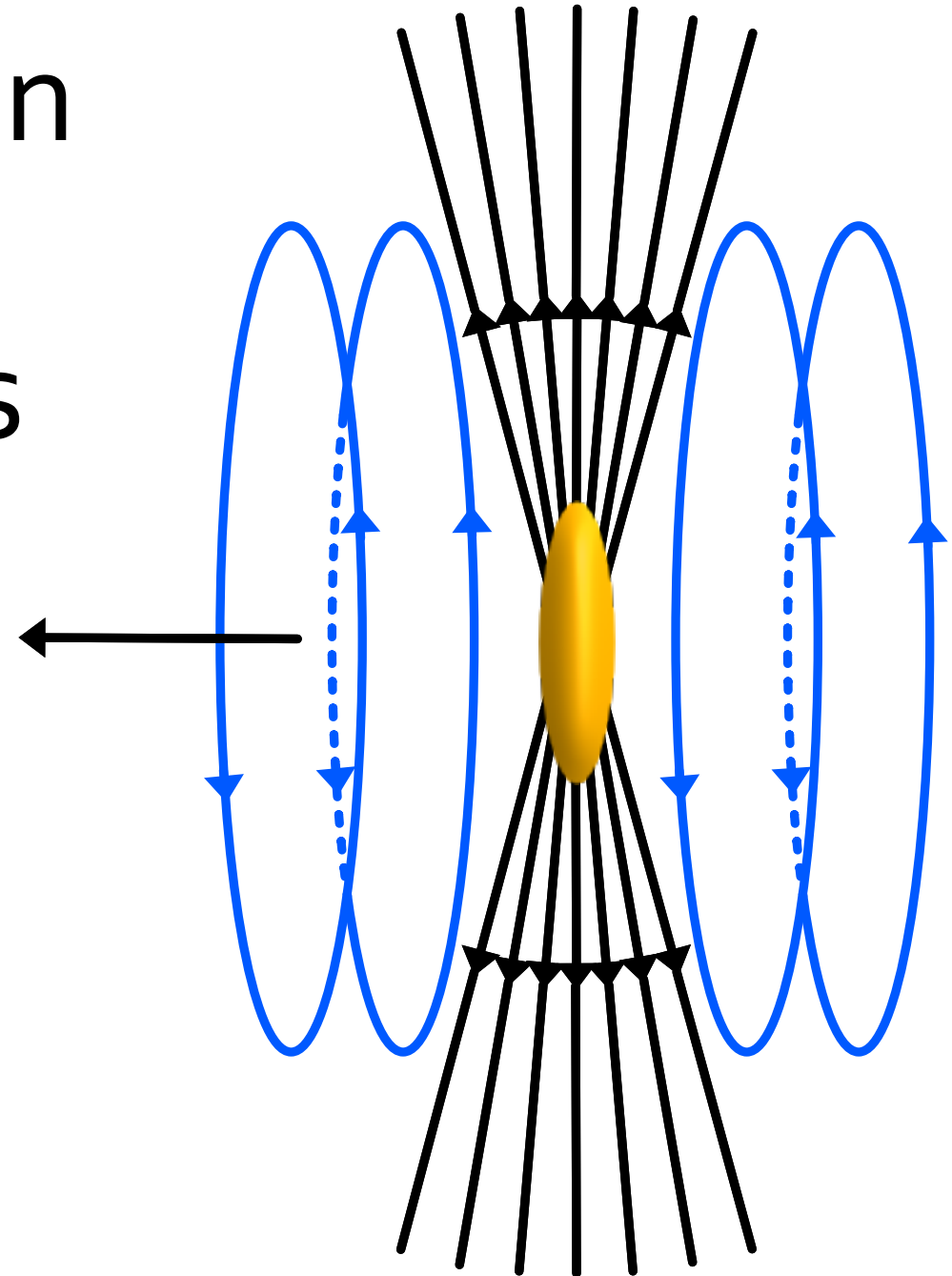
Effects of Strong Fields in Ultra-Peripheral and Peripheral A+A collisions

Daniel Brandenburg

Brookhaven National Lab(CFNS) : Goldhaber Fellow

RHIC & AGS Users' Meeting 2020

October 22nd, 2020 (via ZOOM)



Motivation for Directly Measuring the Magnetic Field

Predicted emergent magnetohydrodynamical phenomena of Quantum Chromodynamics

- Manifestations require ultra-strong magnetic fields
- E.g. **Chiral Magnetic Effect**
- Major goal of RHIC heavy-ion program
 - Dedicated Isobar run in 2018

Dima Kharzeev's Quark Matter 2019 talk:

**Absent in
Maxwell theory!**

$$\vec{J} = \frac{e^2}{2\pi^2} \mu_5 \vec{B}$$

Coefficient is fixed by
the chiral anomaly, no
corrections

5

K.Fukushima, DK, H.Warringa,
"Chiral magnetic effect" PRD'o8

NEED TO KNOW THE MAGNETIC FIELD FOR QUANTITATIVE STUDIES

DK, L.McLerran, H.Warringa NPA'o

Chiro-genesis in Heavy Ion Collisions

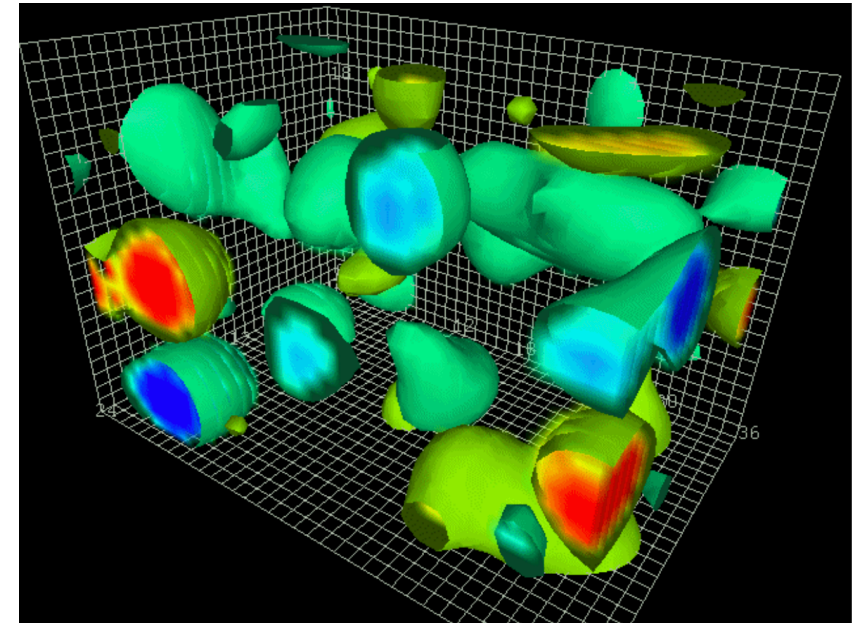


Image: D. Leinweber

Ultra-Relativistic Heavy-Ion Collisions

Ultra-relativistic charged nuclei produce highly Lorentz contracted electromagnetic field

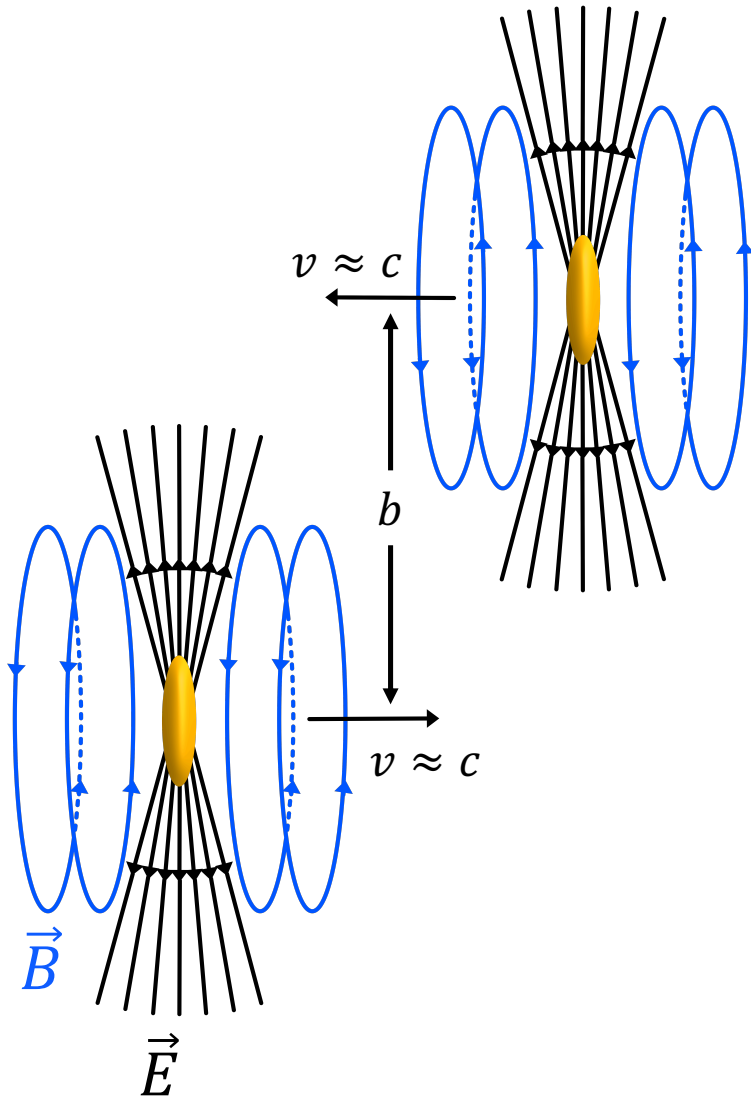
$Z\alpha \approx 1 \rightarrow$ High photon density

Ultra-strong electric and magnetic fields:

\rightarrow Expected magnetic field strength $\vec{B} \approx 10^{14} - 10^{16} \text{ T}$

Skokov, V., et. al. *Int. J. Mod. Phys. A* 24 (2009): 5925–32

**Study unique features of QED
under extreme conditions**

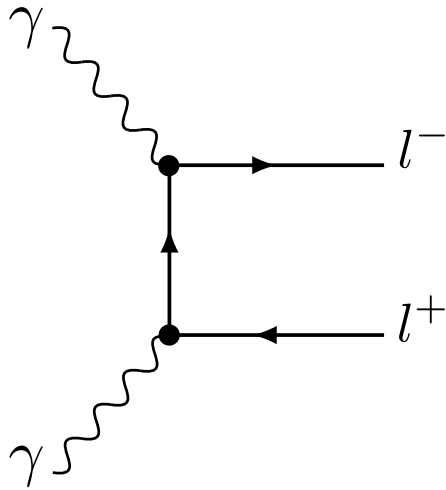


Photon-Photon fusion (Breit-Wheeler Process)

Weizsäcker, C. F. v. *Zeitschrift für Physik* 88 (1934): 612

Weizäcker-Williams *Equivalent Photon Approximation* (EPA)

→ In a specific phase space, transverse EM fields can be quantized as a flux of **real photons**



Photon-photon fusion into
lepton anti-lepton pair
**Characterized by $l^+ l^-$ pair
with very small p_T**

Photon number density related to field strength
(Poynting Vector)

$$n \propto \vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B} \approx |\vec{E}|^2 \approx |\vec{B}|^2$$

Traditional EPA calculations (e.g. STARLight[1])
have predicted cross section correctly for decades
→ **so what is new?**

[1] S. R. Klein, et. al. *Comput. Phys. Commun.* 212 (2017) 258

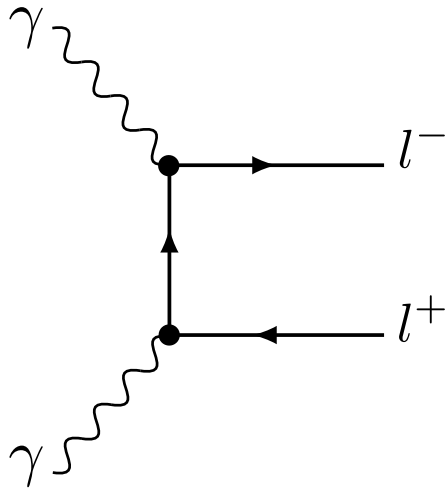
Daniel Brandenburg | BNL (CFNS) / SDU

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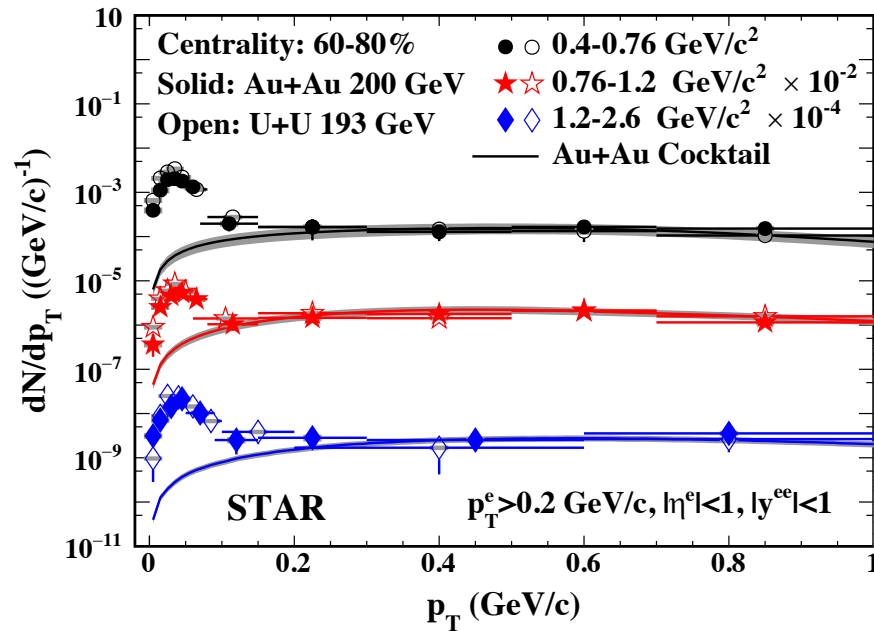
What's new?

1. Pair p_T shows impact parameter dependence
→ Sensitivity to the field mapping
2. Azimuthal angle correlation in daughter leptons
→ Quantum position-momentum correlations

Use these to experimentally constrain the initial
EM fields

Surprising result in Peripheral Collisions

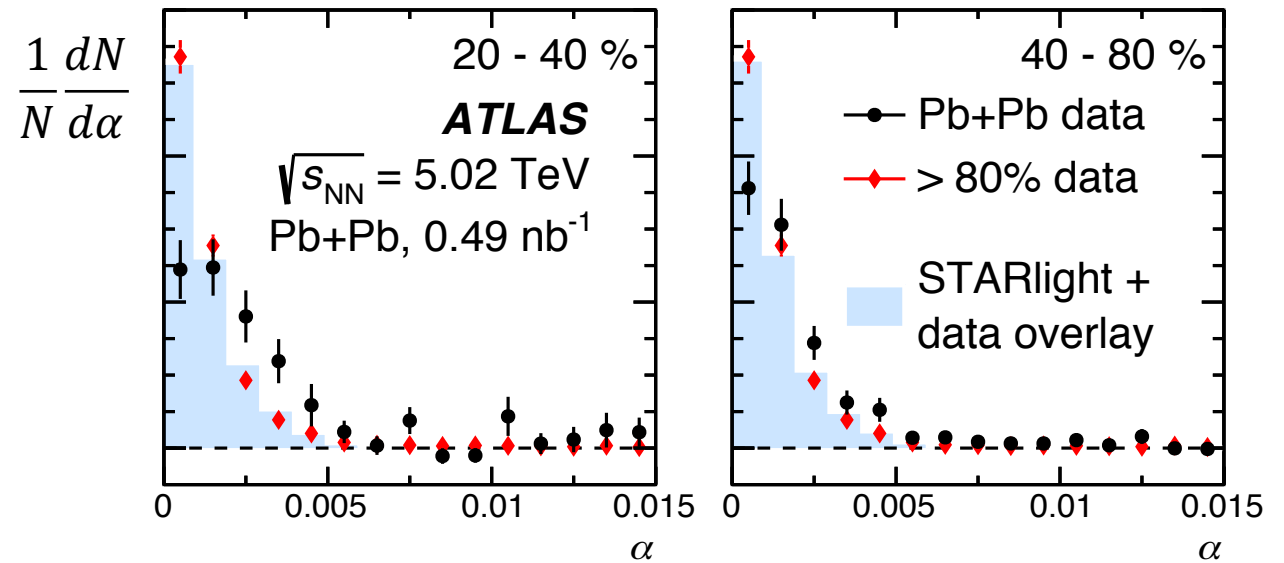
STAR Measurement of e^+e^- at low p_T



Strong excess at low p_T over hadronic cocktail observed in peripheral collisions

[1] STAR, Phys. Rev. Lett. 121 (2018) 132301

ATLAS Measurement of $\mu^+\mu^-$ at small acoplanarity



Pairs with small acoplanarity (proxy to pair p_T) observed in peripheral collisions

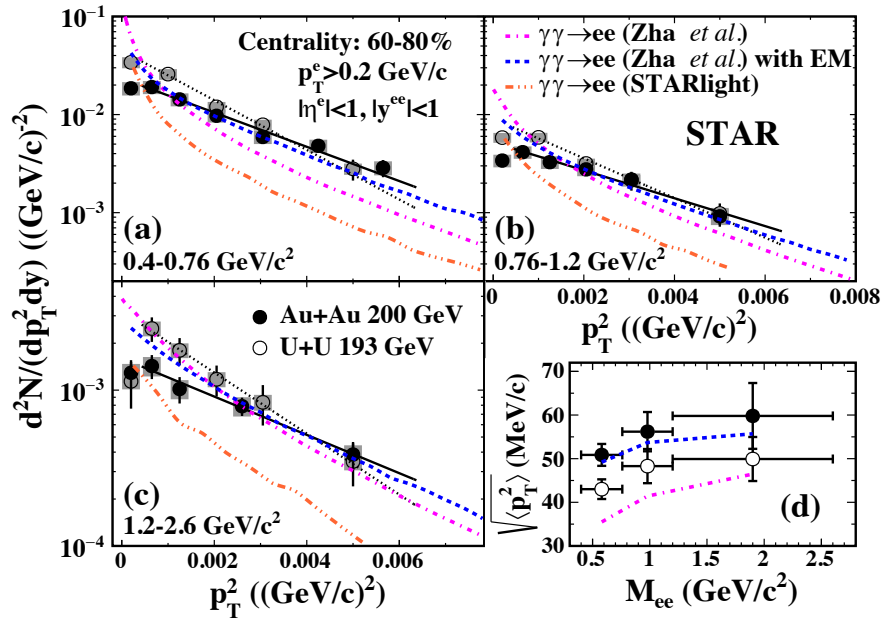
$$\alpha = 1 - \frac{|\phi^+ - \phi^-|}{\pi} \propto \frac{p_T}{M}$$

[2] ATLAS, Phys. Rev. Lett. 121, 212301 (2018)

→ Photon-photon fusion even in peripheral collisions with hadronic overlap?

Surprising result in Peripheral Collisions

STAR Measurement of e^+e^- at low p_T



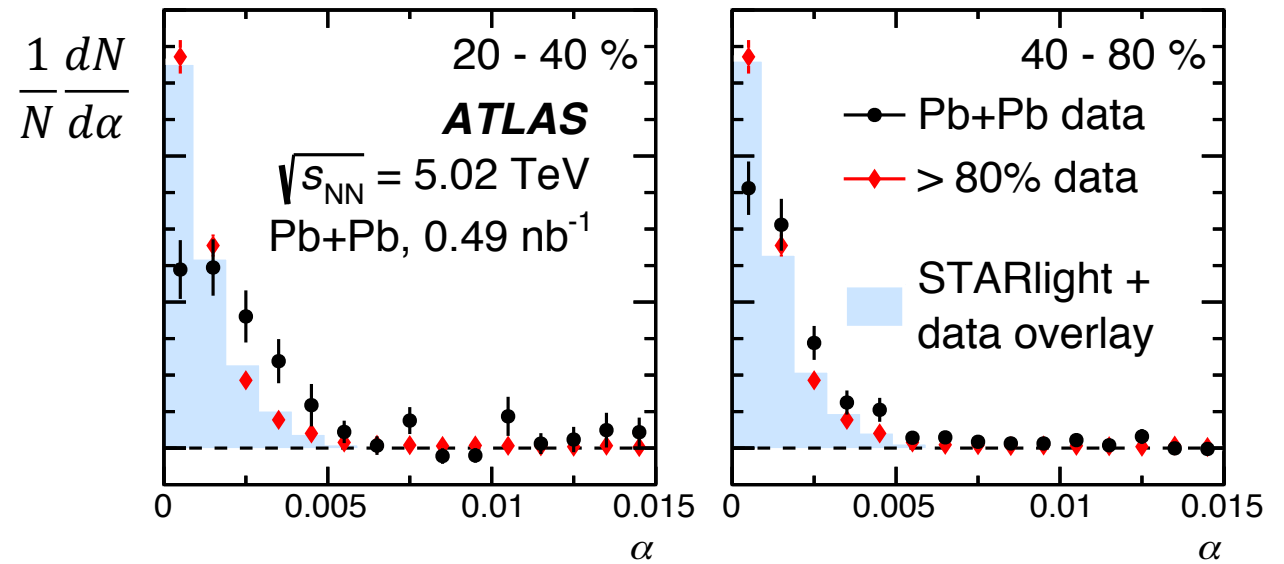
Strong excess at low p_T over hadronic cocktail observed in peripheral collisions

[1] STAR, Phys. Rev. Lett. 121 (2018) 132301

→ Photon-photon fusion even in peripheral collisions with hadronic overlap?

Traditional EPA calculation cannot describe p_T or α distribution

ATLAS Measurement of $\mu^+\mu^-$ at small acoplanarity



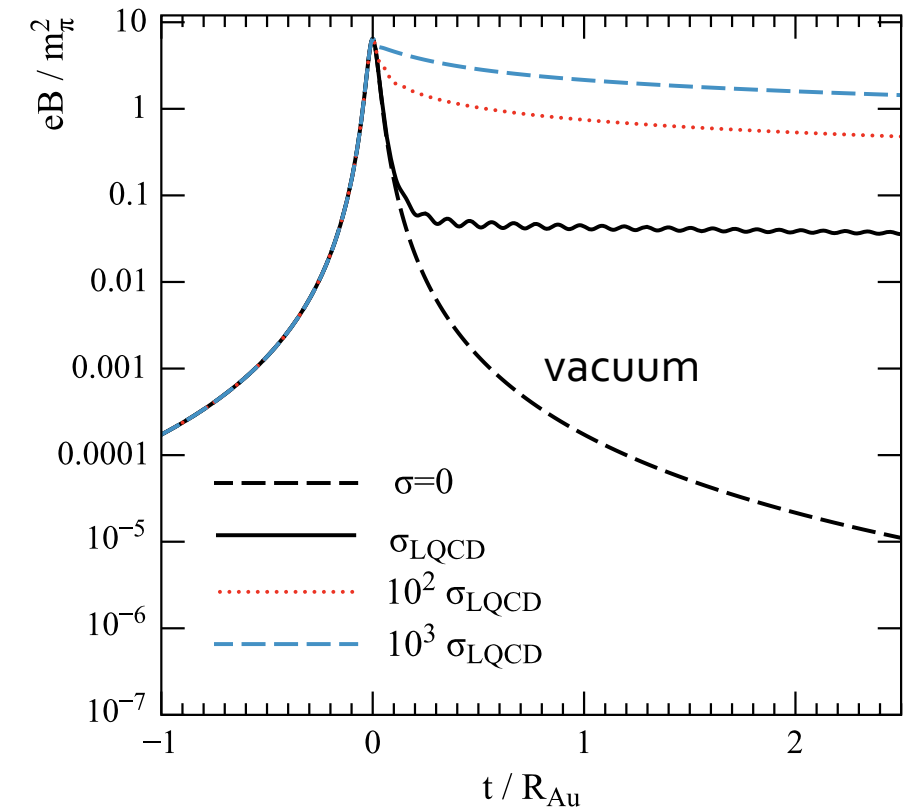
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[2] ATLAS, Phys. Rev. Lett. 121, 212301 (2018)

Is the broadening due to final state, medium effects?

- Idea: Extremely small $P_{\perp} \rightarrow$ easily deflected by relatively small perturbations
- Two proposals from different groups:
 1. Lorentz-Force bending due to long-lived magnetic field [1] STAR, Phys. Rev. Lett. 121 (2018) 132301
 2. Coulomb scattering through QGP medium [2] S. R. Klein, et. al, Phys. Rev. Lett. 122, (2019), 132301
[3] ATLAS, Phys. Rev. Lett. 121 (2018), 212301



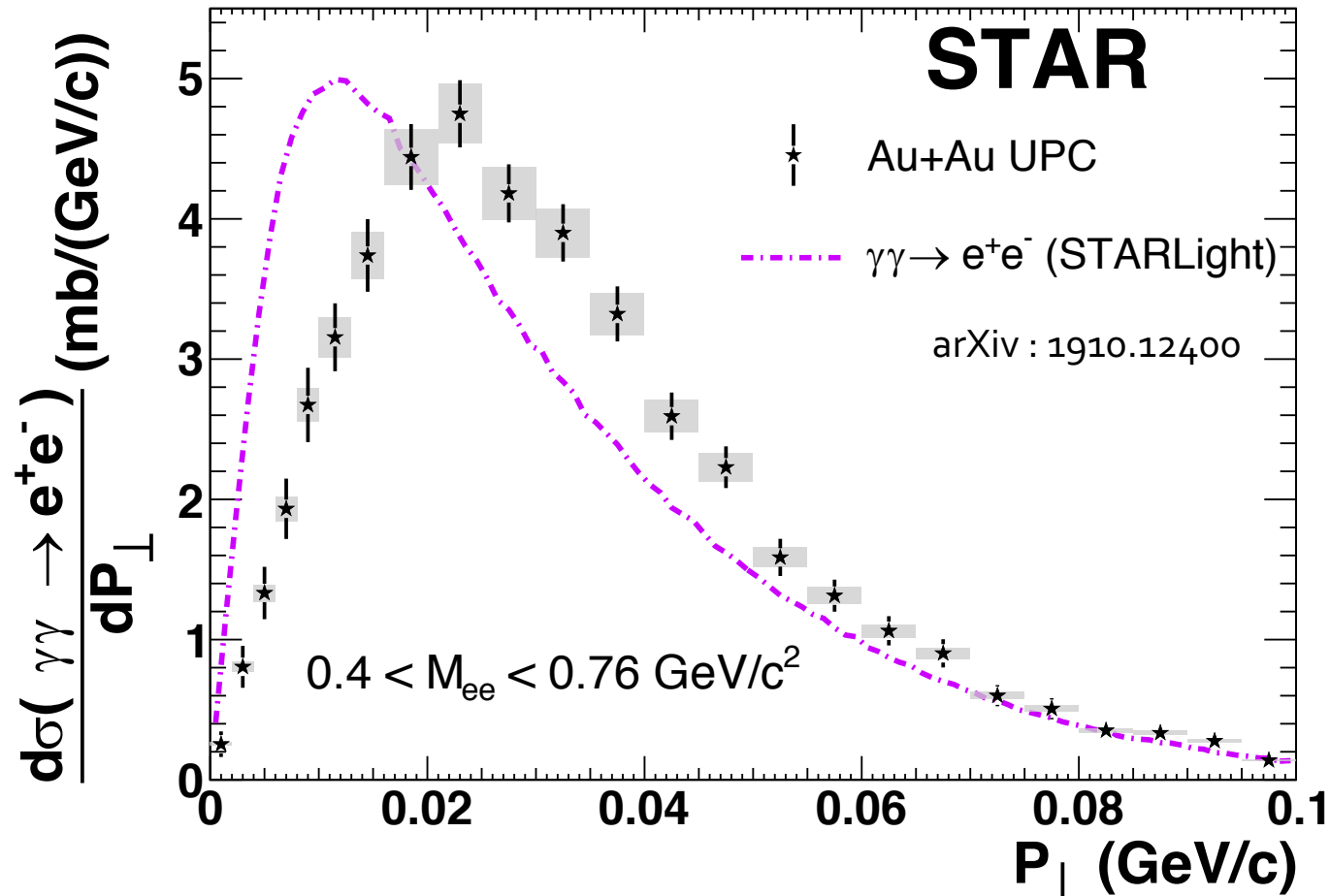
L. McLerran, V. Skokov, Nuclear Physics A 929 (2014) 184–190

Equivalent Photon Approximation

- Traditional Equivalent Photon Approximation (EPA) has been used to describe cross section **successfully** ($\sim \pm 30\%$ level) for years
- ✓ Take impact parameter (b) into account for photon flux
- ✗ BUT, treats photons as plane waves with $\vec{k} = k\hat{z}$
 - In this treatment photon p_T must result from virtuality
→ **No b -dependence on kinematics (p_T, α , etc)**
- Until recently there was no data to test the validity of these assumptions
 - E.g. past ATLAS UPC measurements agree with STARLight but resolution effects are significant, obscure the physics
 - Past STAR measurements – insufficient statistical precision

[1] S. R. Klein, et. al. *Comput. Phys. Commun.* 212 (2017) 258

$$d\sigma(\gamma\gamma \rightarrow e^+e^-)/dP_{\perp}$$



QED and STARLight are scaled to match measured $\sigma(\gamma\gamma \rightarrow e^+e^-)$

STARLight: S. R. Klein, et. al. *Comput. Phys. Commun.* 212 (2017) 258

QED : W. Zha, J.D.B., Z. Tang, Z. Xu arXiv:1812.02820 [nucl-th]

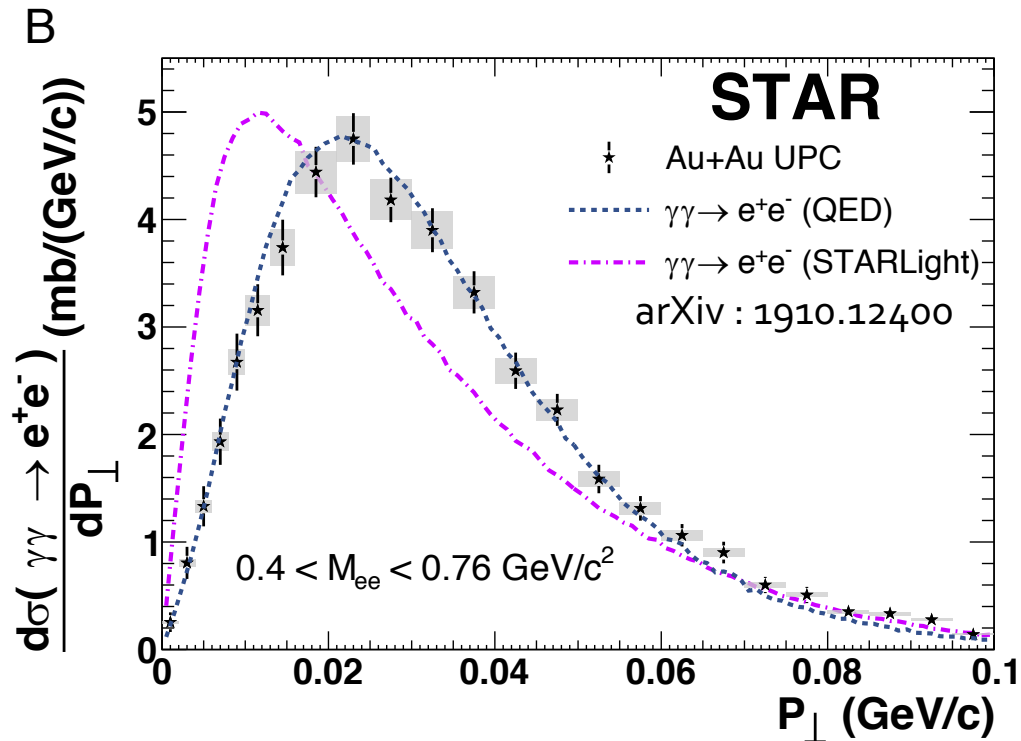
- STAR's excellent p_T resolution → directly measure pair p_T
- High precision data – **test various theory predictions/assumptions**

○ STARLight predicts significantly lower $\langle P_{\perp} \rangle$ than seen in data

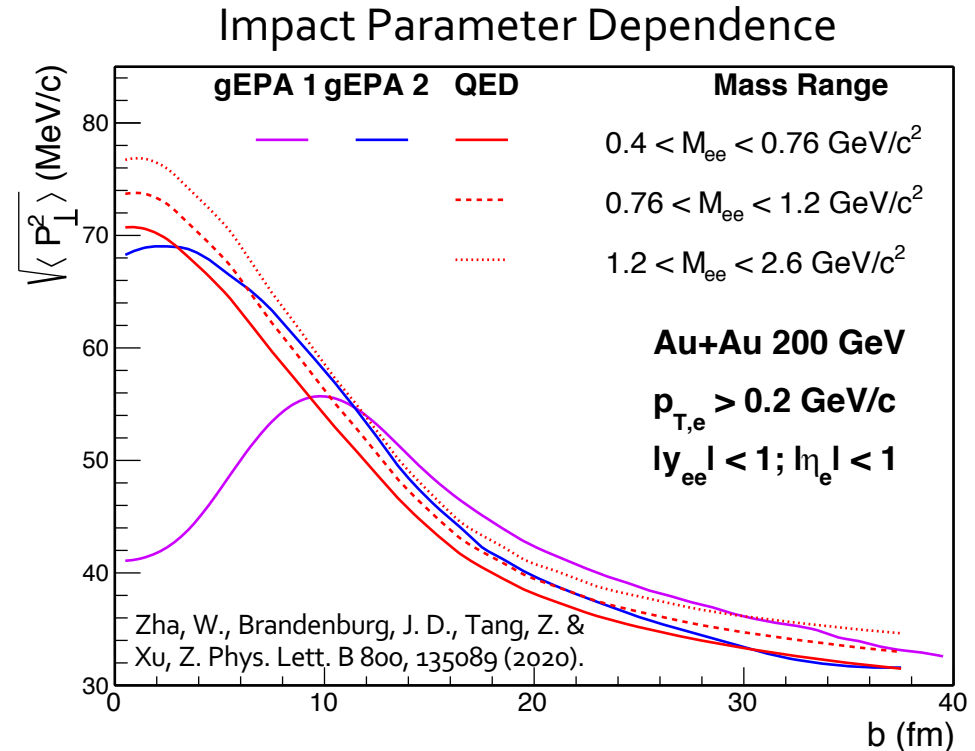
○ Is the increased P_{\perp} observed due to significant virtuality?

○ Let's look at how the calculation is done in the lowest order QED case

Pair p_T and impact parameter



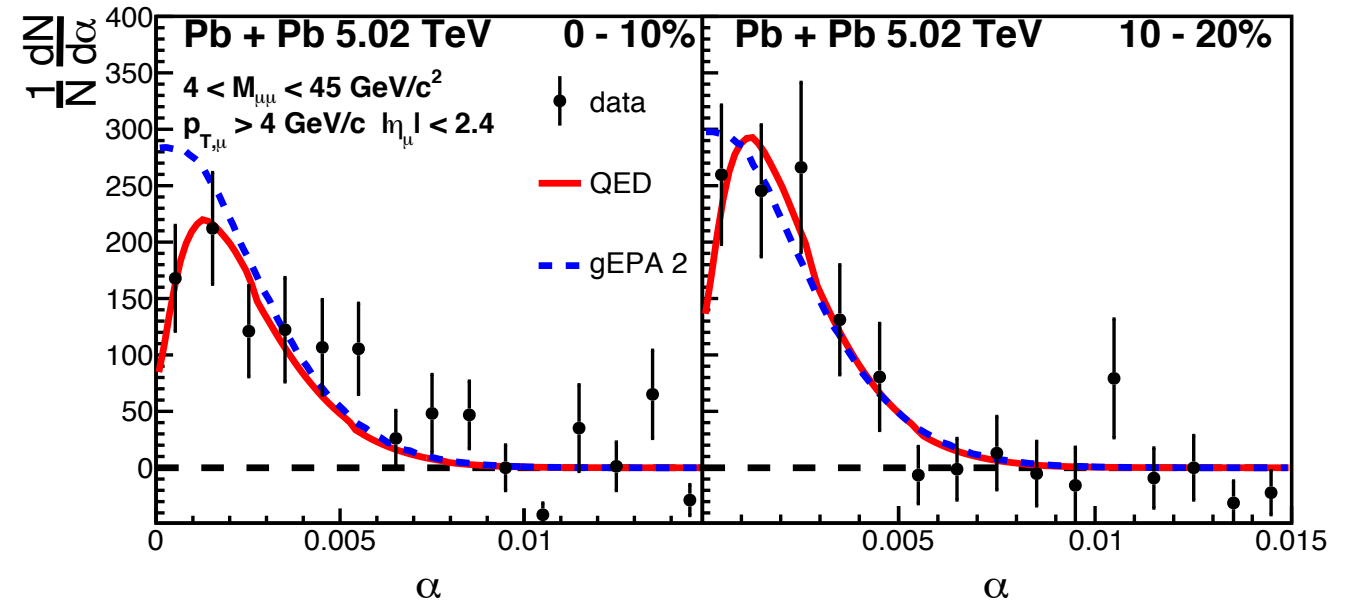
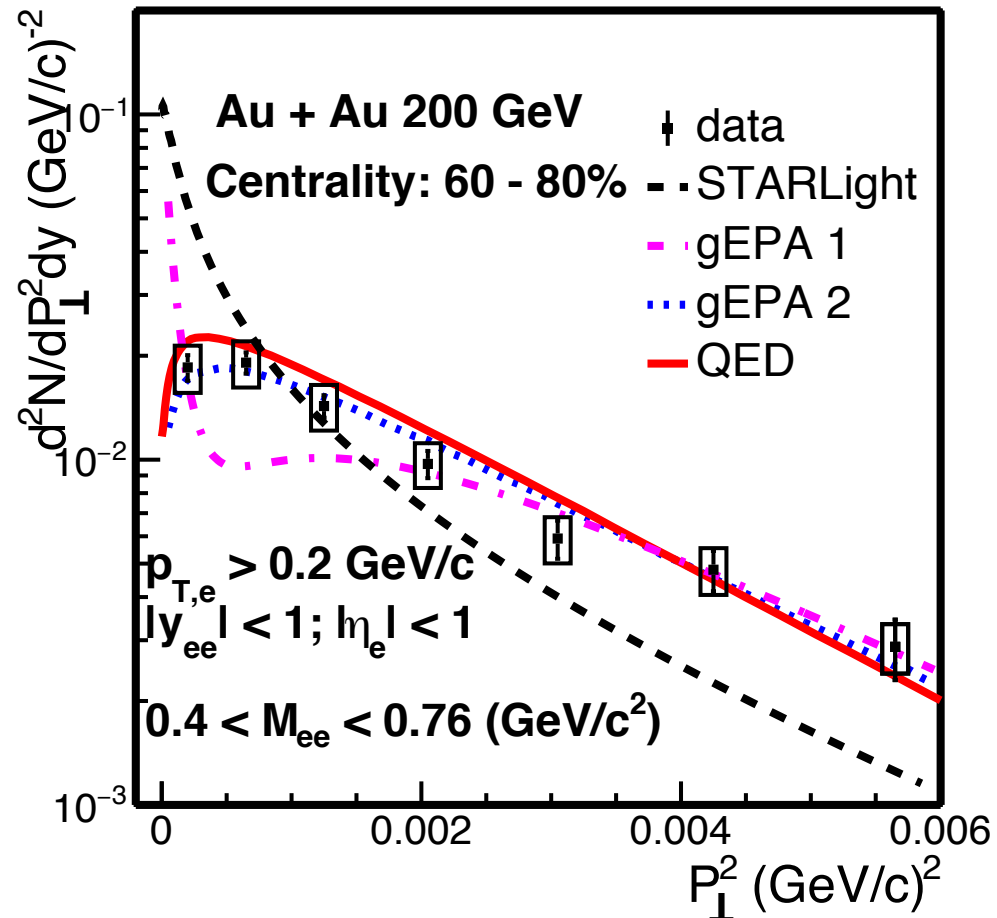
QED (and gEPA parameterization) describe data
 Larger $\langle P_{\perp} \rangle$ from impact parameter dependence
not a result of significant photon virtuality



Note: gEPA1 vs. gEPA2 : gEPA2 includes phase term to approximate full QED result

- QED calculation predicts impact parameter dependence → **dependence on the overlapping field strengths. Can the QED describe the peripheral data?**

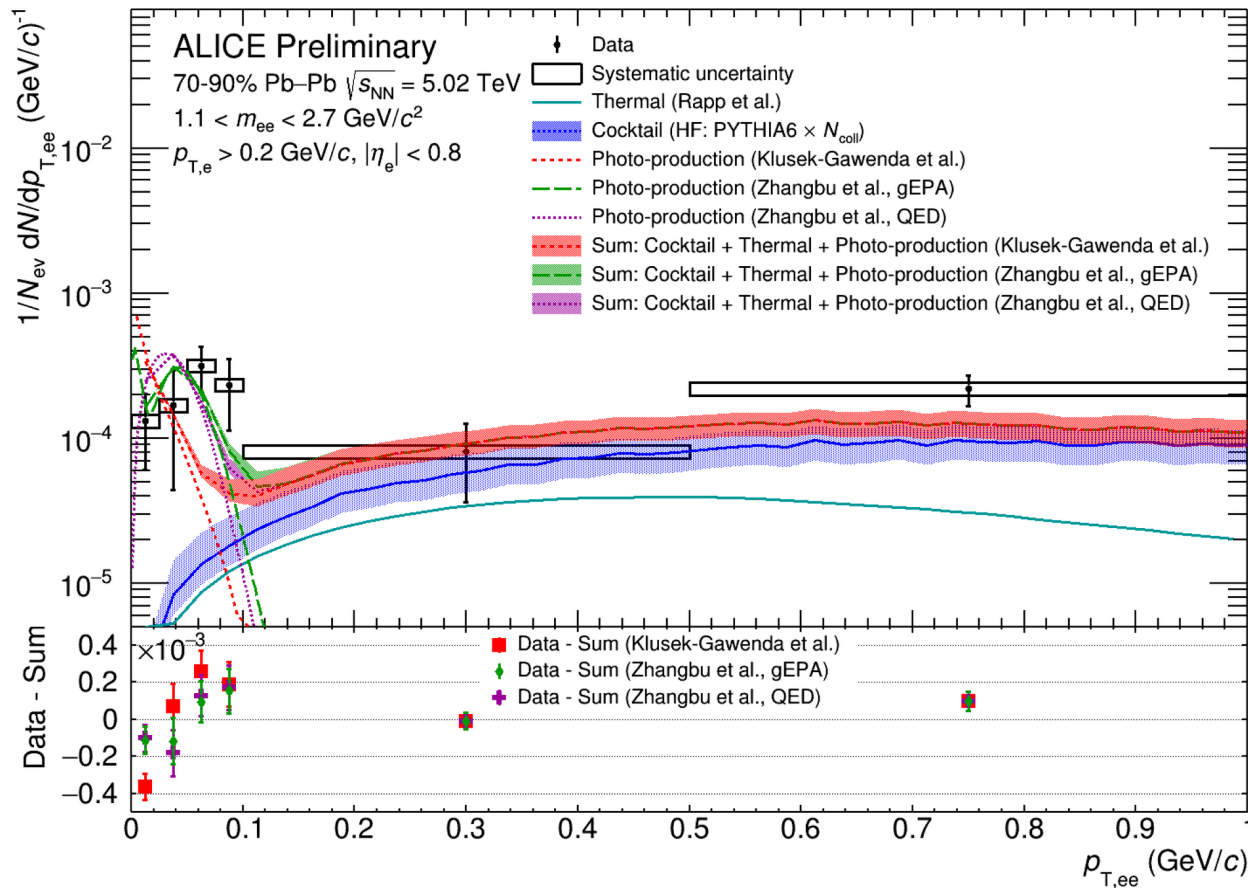
QED Calculation & Peripheral Data



- Peripheral data from both STAR and ATLAS are well described by QED calculation
- ATLAS has newer high precision data

Physics Letters B 800 (2020) 135089

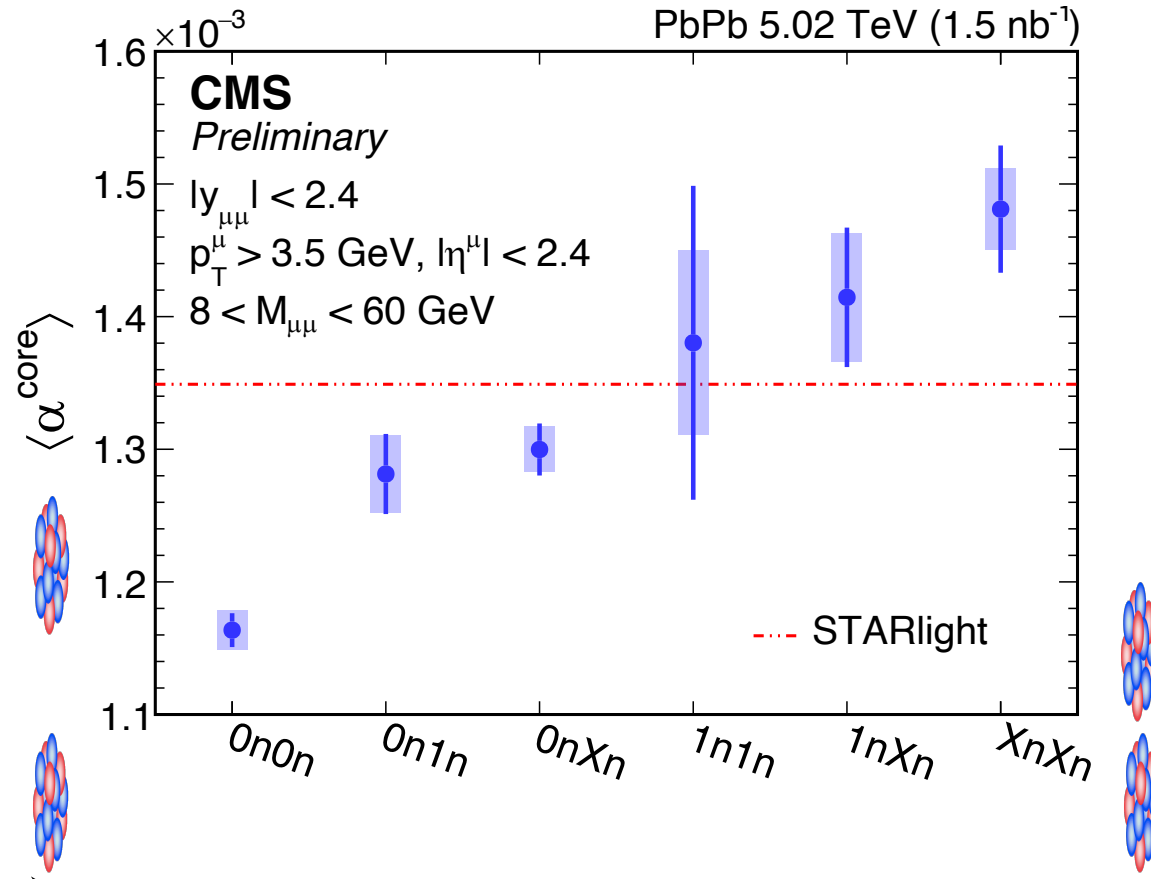
QED Calculation & Peripheral Data



- Similar measurement by ALICE in 70 – 90% central collisions
- Low statistics $\rightarrow p_T$ distribution favors QED calculation over traditional EPA

ALICE Preliminary from QM19

QED Calculation & CMS UPC Data



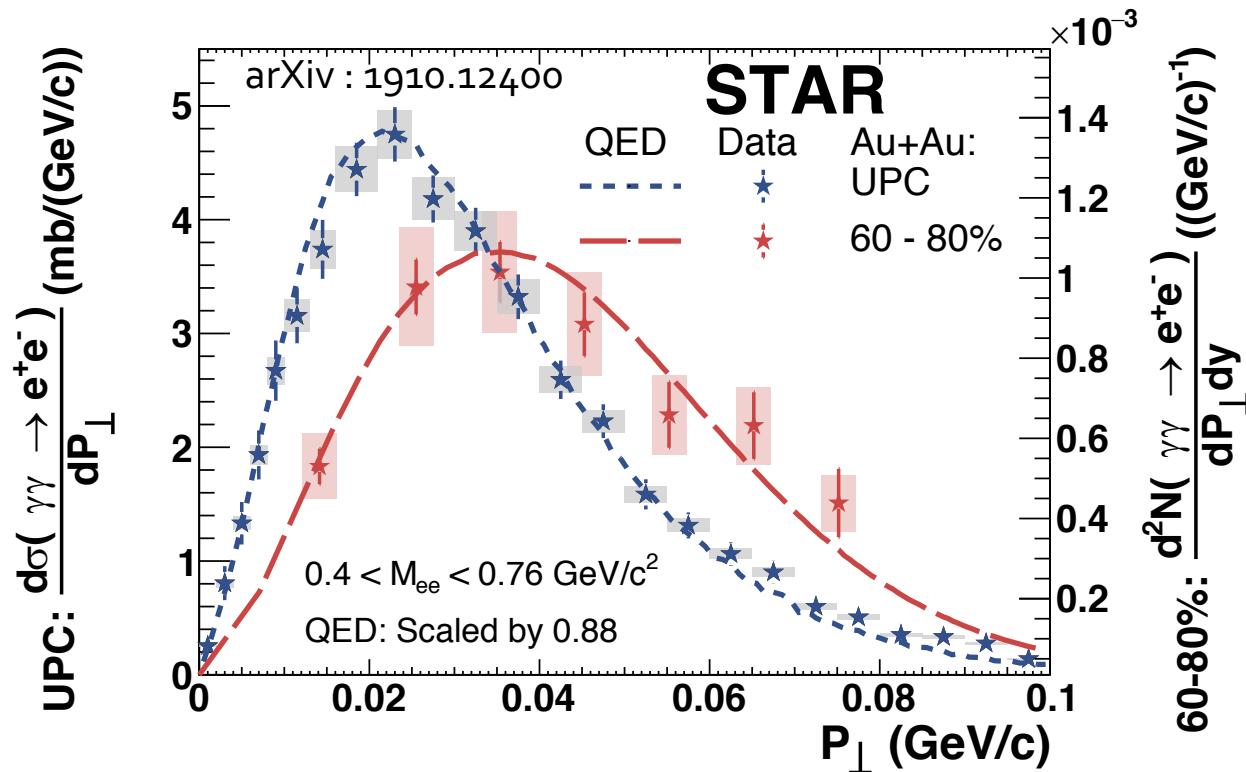
ShuaiYang, CMS Preliminary from HP2020

- CMS measured α for various impact parameter ranges by tagging the neutron emission
- Acoplanarity shows impact parameter dependence in UPC – purely initial state effect
- QED calculation also describes this data well,

see [arxiv:2006.07365](https://arxiv.org/abs/2006.07365)

$\gamma\gamma \rightarrow e^+e^-$: UPC vs. Peripheral

[1] STAR, Phys. Rev. Lett. 121 (2018) 132301
 [2] S. R. Klein, et. al, Phys. Rev. Lett. 122, (2019), 132301
 [3] ATLAS Phys. Rev. Lett. 121 (2018), 212301



Characterize difference in spectra via $\sqrt{\langle P_\perp^2 \rangle}$

$\sqrt{\langle P_\perp^2 \rangle}$ (MeV/c)	UPC Au+Au	60-80% Au+Au
Measured	38.1 ± 0.9	50.9 ± 2.5
QED	37.6	48.5
b range (fm)	≈ 20	$\approx 11.5 - 13.5$

- Leading order QED calculation of $\gamma\gamma \rightarrow e^+e^-$ describes both spectra ($\pm 1\sigma$)
- Best fit for spectra in 60-80% collisions found for QED shape plus 14 ± 4 (stat.) ± 4 (syst.) MeV/c broadening
- Proposed as a probe of trapped magnetic field or Coulomb scattering in QGP [1-3]

QED describes p_T spectra in terms of the initial fields!

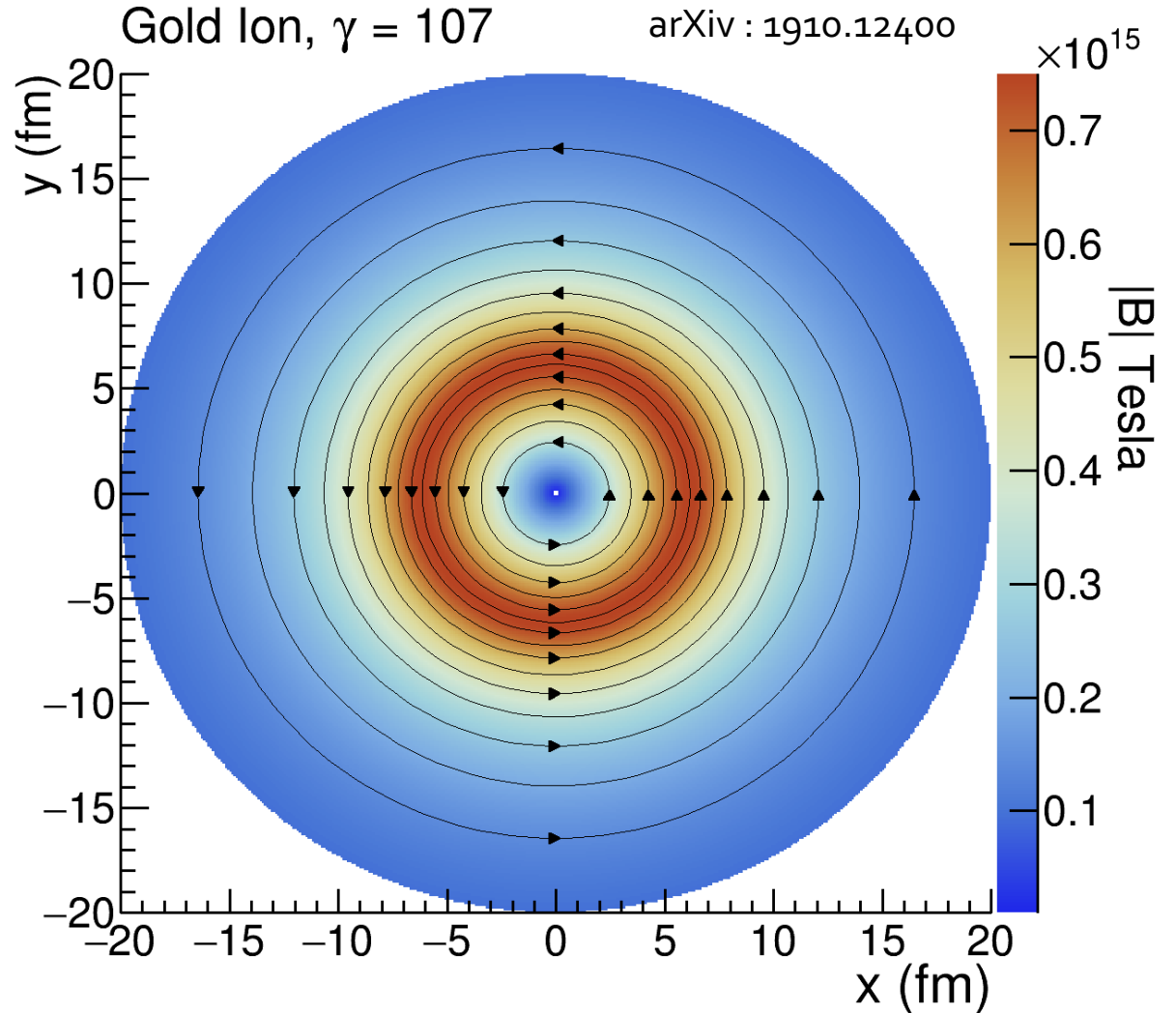
Maybe there is still room for final state effects – test with new ATLAS results (QM19)

Connection to the Initial Magnetic Field

Magnetic field strength and spatial distribution:

- Impact parameter dependence of P_{\perp}
- Amplitude of azimuthal angular modulation

QED calculations for Breit-Wheeler ($\gamma\gamma \rightarrow e^+e^-$) process that use the field map (to the right) describe data $\pm 1\sigma$

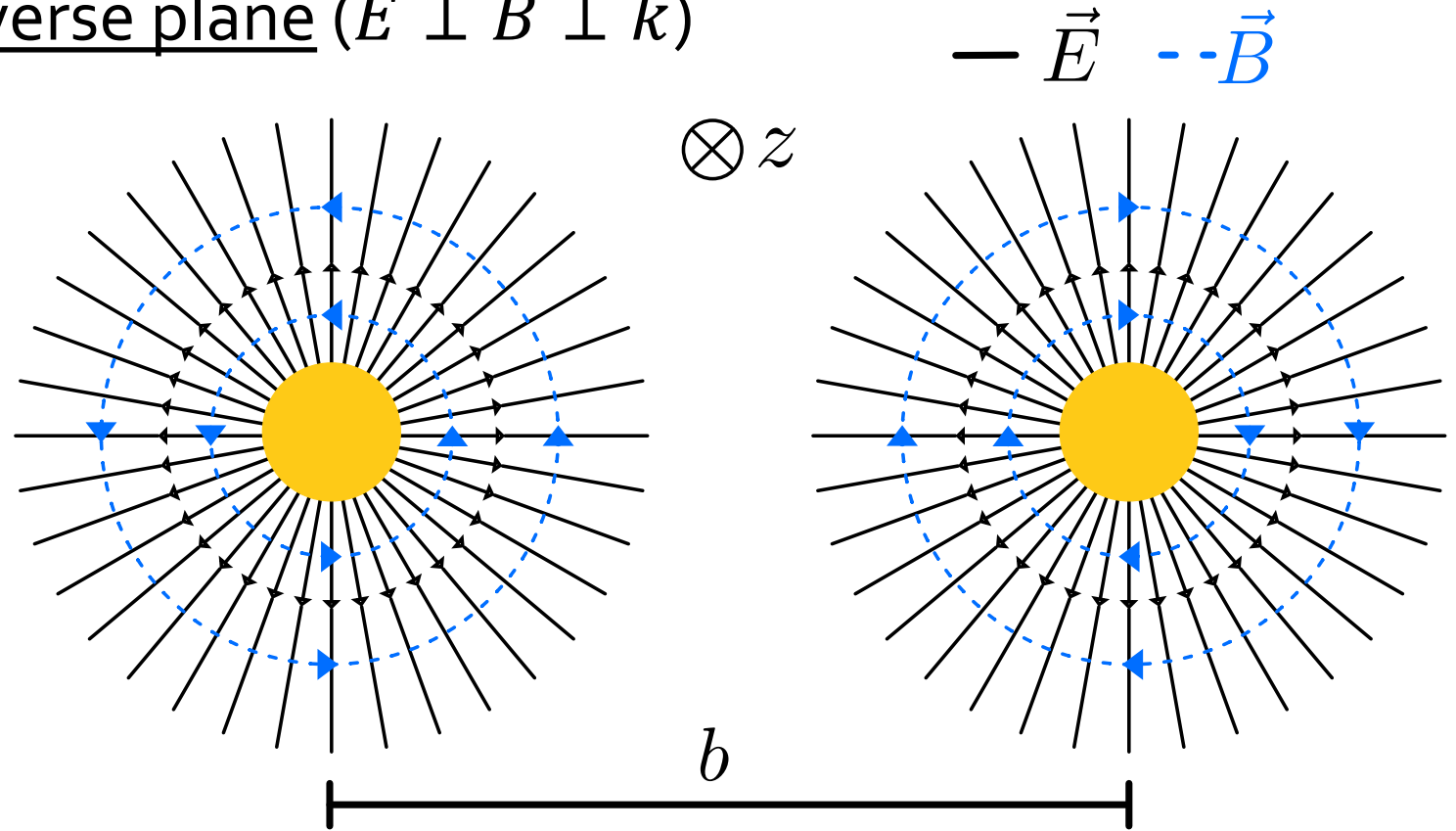


Peak value for single ion: $|B| \approx 0.8 \times 10^{15}$ Tesla $\approx 10,000\times$ stronger than Magnetars

Transverse linearly polarized photons

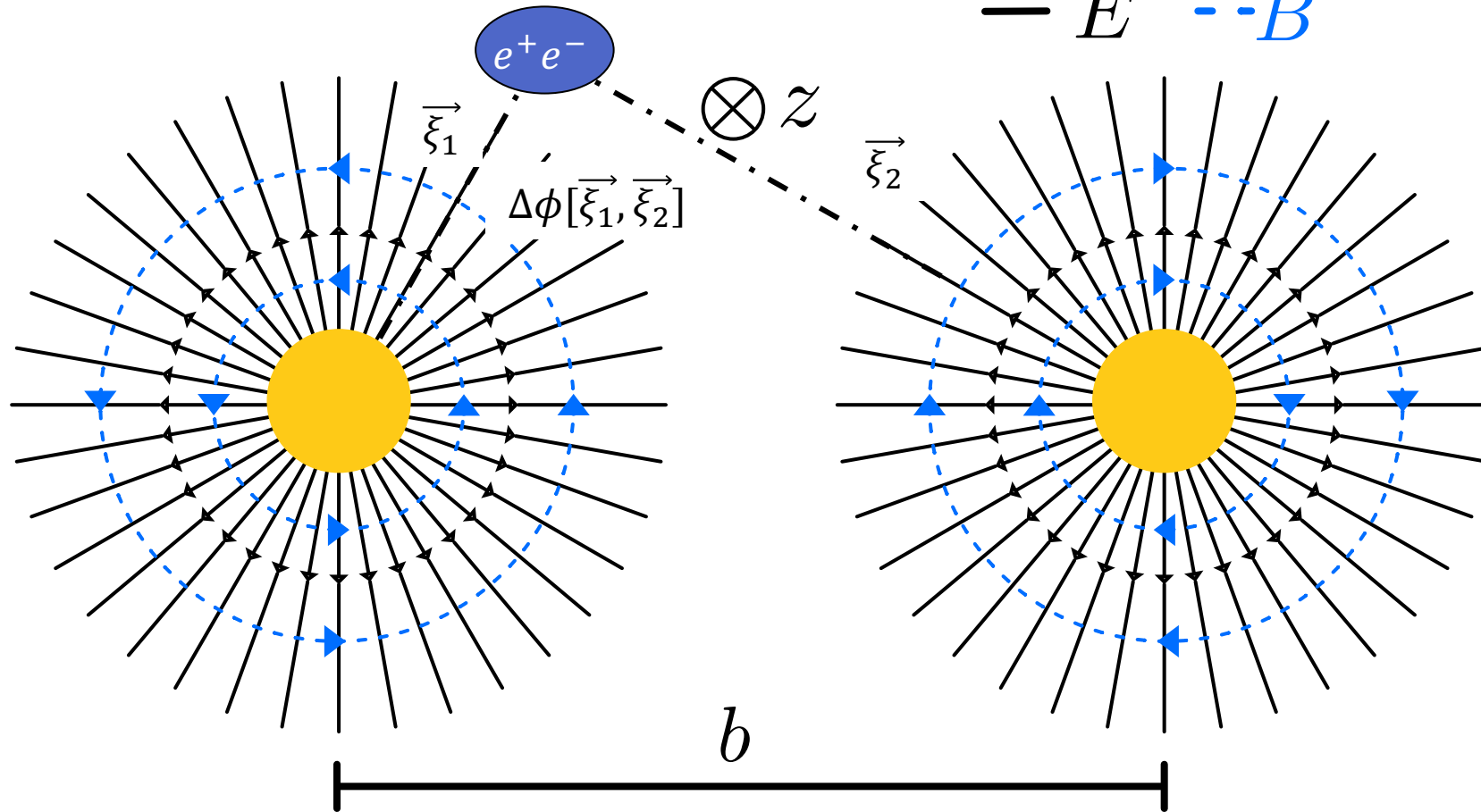
- Lorentz contraction of EM fields → Quasi-real photons should be linearly polarized in transverse plane ($\vec{E} \perp \vec{B} \perp \vec{k}$)

- Polarization vector : aligned radially with the “emitting” source
- Well defined in the photon position eigenstates
- In general event average, washes out polarization effects, since \vec{b} is random



Transverse linearly polarized photons

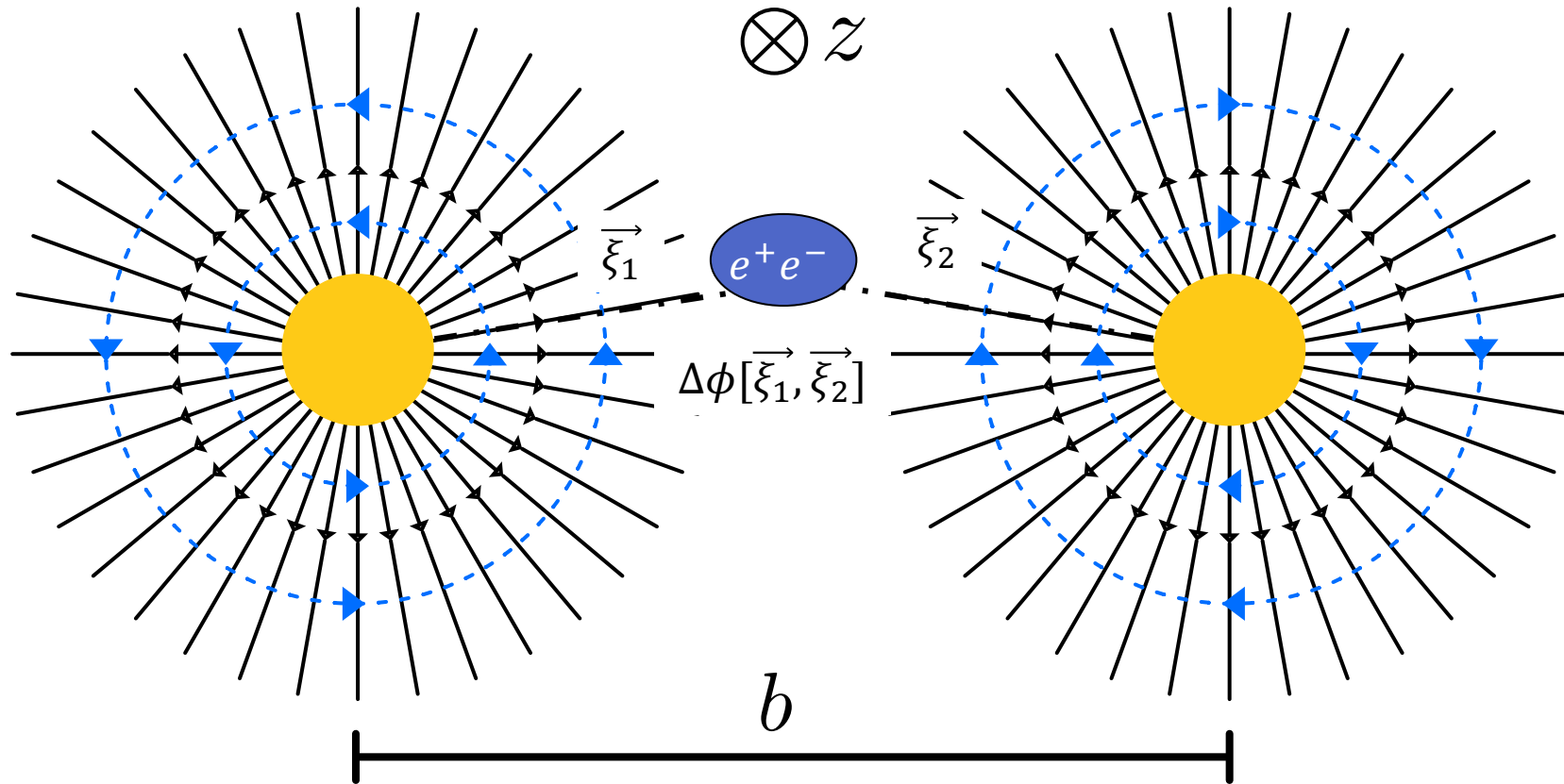
$$- \vec{E} \quad - - \vec{B}$$



- Angle between photon polarizations depends on location of produced pair

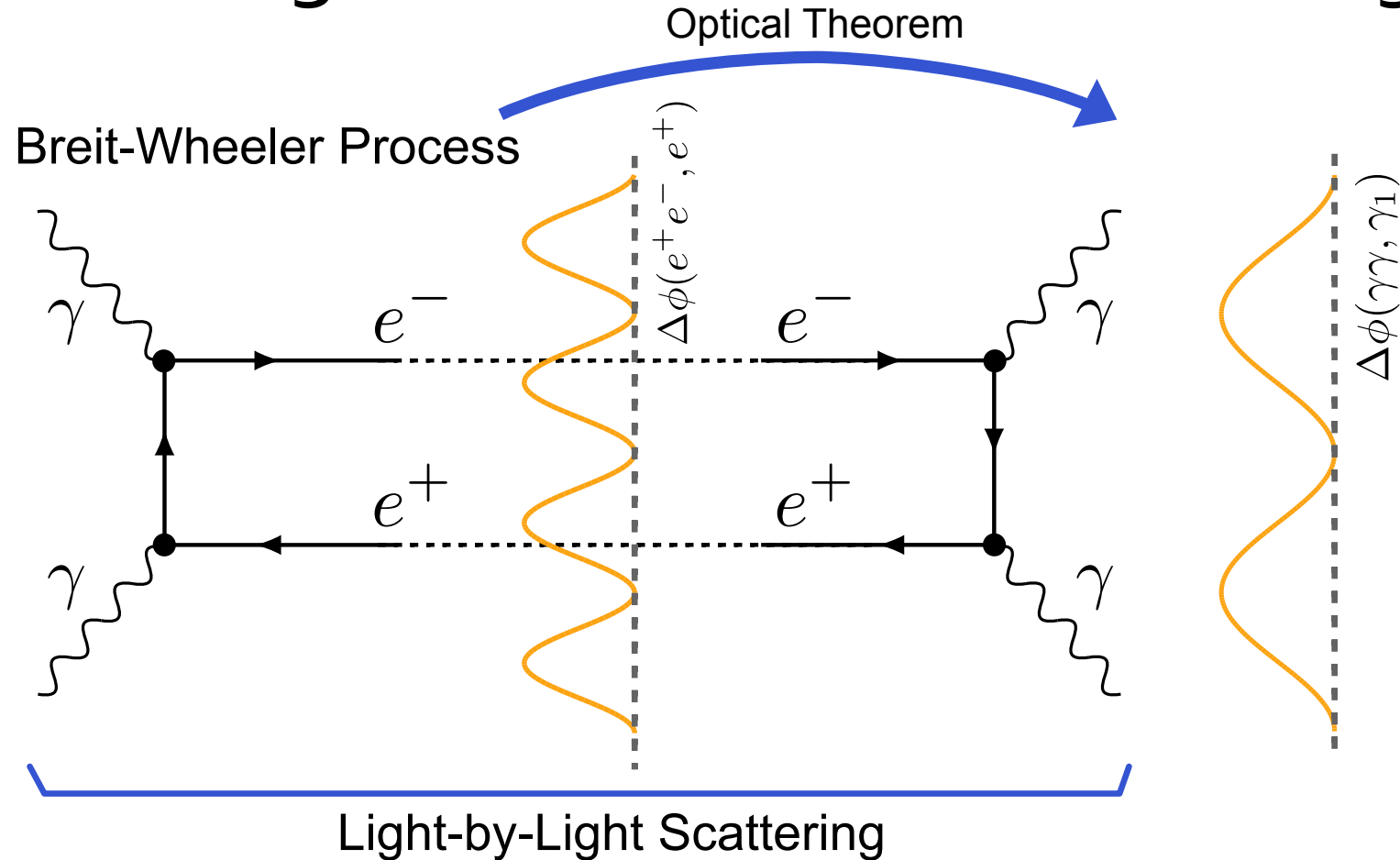
Transverse linearly polarized photons

$$- \vec{E} \quad - - \vec{B}$$



- Angle between photon polarizations depends on location of produced pair

Experimental Signature of Vacuum Birefringence



Recently realized, $\Delta\sigma = \sigma_{\parallel} - \sigma_{\perp} \neq 0$ leads to a **$\cos(4\Delta\phi)$ modulation** in polarized $\gamma\gamma \rightarrow e^+e^-$ [1]

The corresponding vacuum LbyL scattering[2] displays a **$\cos(2\Delta\phi)$ modulation**

[1] C. Li, J. Zhou, Y.-j. Zhou, Phys. Lett. B 795, 576 (2019)

[2] Harland-Lang, L. A., Khoze, V. A. & Ryskin, M. G. Eur. Phys. J. C 79, 39 (2019).

$$\Delta\phi = \Delta\phi[(e^+ + e^-), (e^+ - e^-)] \\ \approx \Delta\phi[(e^+ + e^-), e^+]$$

Birefringence of the QED Vacuum

[1] C. Li, J. Zhou, Y.-j. Zhou, Phys. Lett. B 795, 576 (2019)
QED calculation: Li, C., Zhou, J. & Zhou, Y. Phys. Rev. D 101, 034015 (2020).

Polarized $\gamma\gamma \rightarrow e^+e^-$ leads to $\cos 4\Delta\phi$ modulations due to quantum space-momentum correlations[1]

$$\Delta\phi = \Delta\phi[(e^+ + e^-), (e^+ - e^-)] \\ \approx \Delta\phi[(e^+ + e^-), e^+]$$

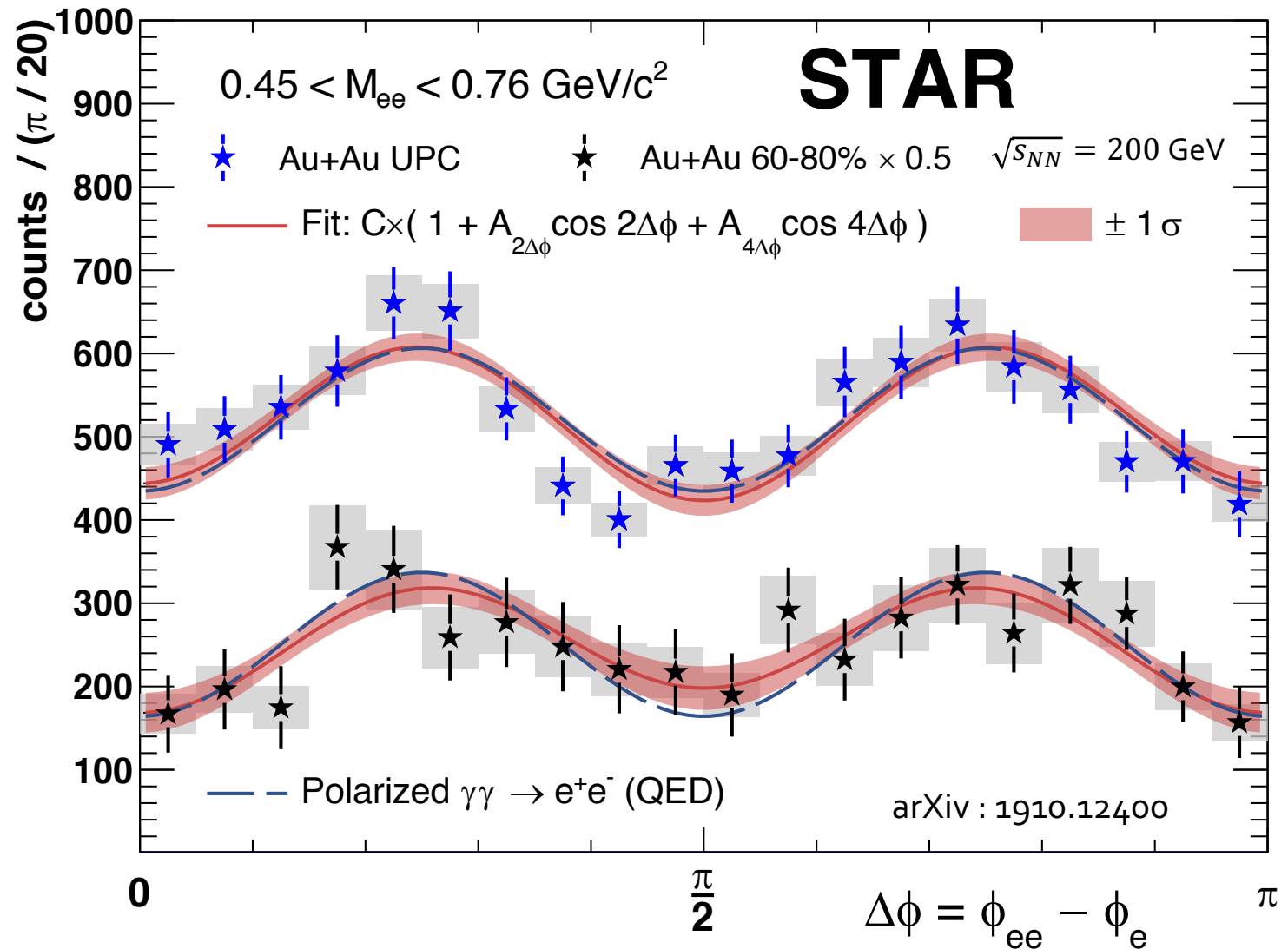
Ultra-Peripheral

Quantity	Measured	QED	χ^2/ndf
$-A_{4\Delta\phi}(\%)$	16.8 ± 2.5	16.5	18.8 / 16

Peripheral (60–80%)

Quantity	Measured	QED	χ^2/ndf
$-A_{4\Delta\phi}(\%)$	27 ± 6	34.5	10.2 / 17

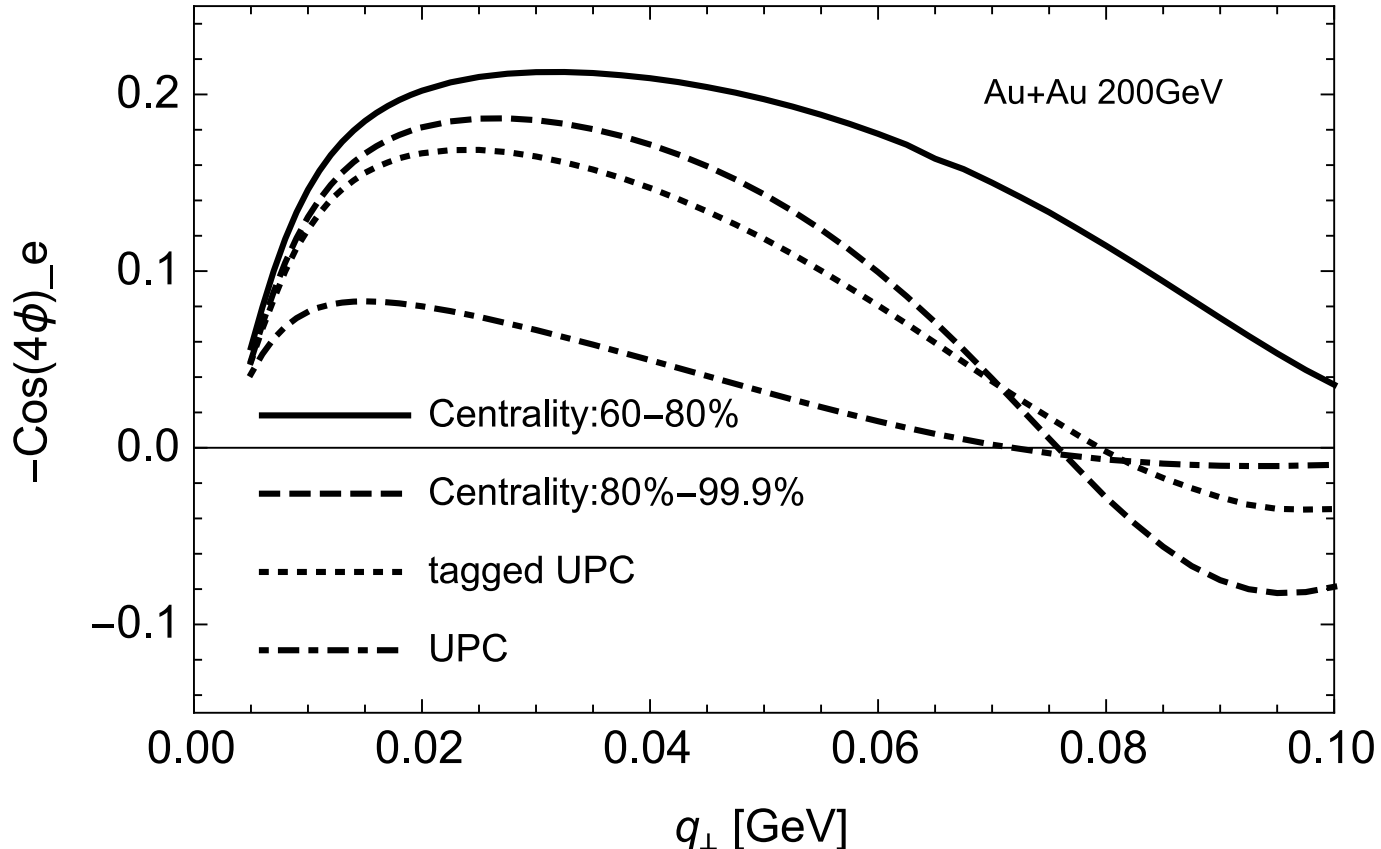
→ First Earth-based observation (6.7 σ level) of vacuum birefringence



Connection to the Initial Magnetic Field

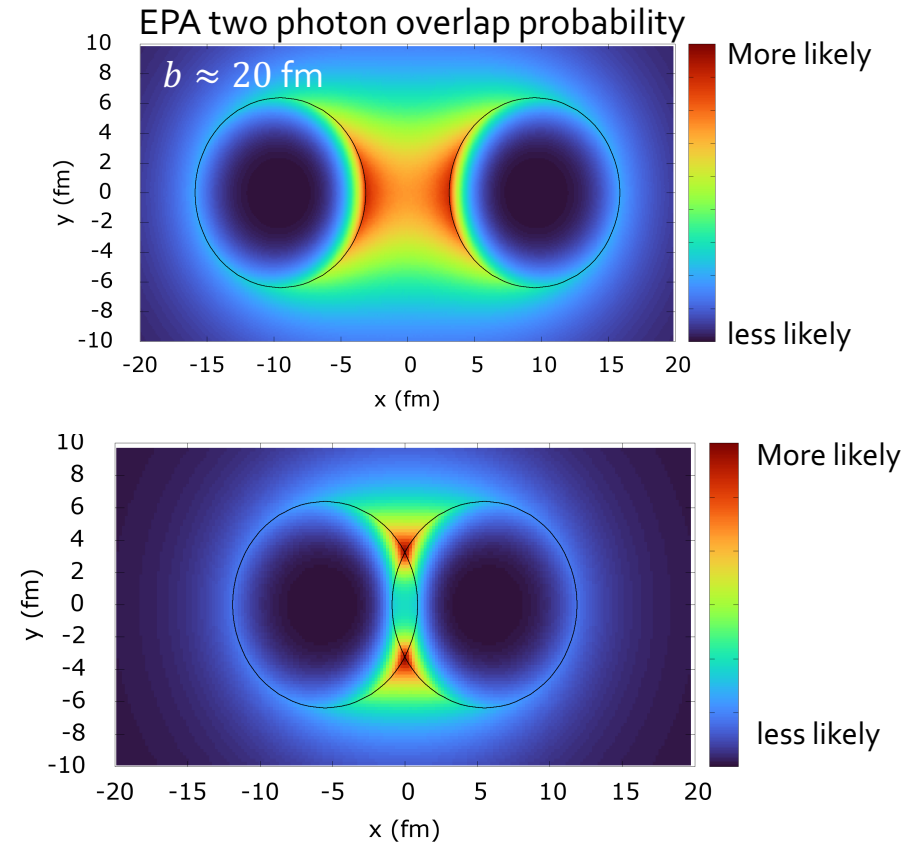
Magnetic field strength and spatial distribution:

Li, C., Zhou, J. & Zhou, Y. Phys. Rev. D 101, 034015 (2020).



- Amplitude of $\cos 4\Delta\phi$ modulation is quite sensitive to field distribution

- Illustration to show that $\Delta\phi[\vec{\xi}_1, \vec{\xi}_2]$ changes with b



Caveat: These do not include $\sigma^{\gamma\gamma \rightarrow l^+l^-}$, integrated over kinematics, only meant as illustration

Summary

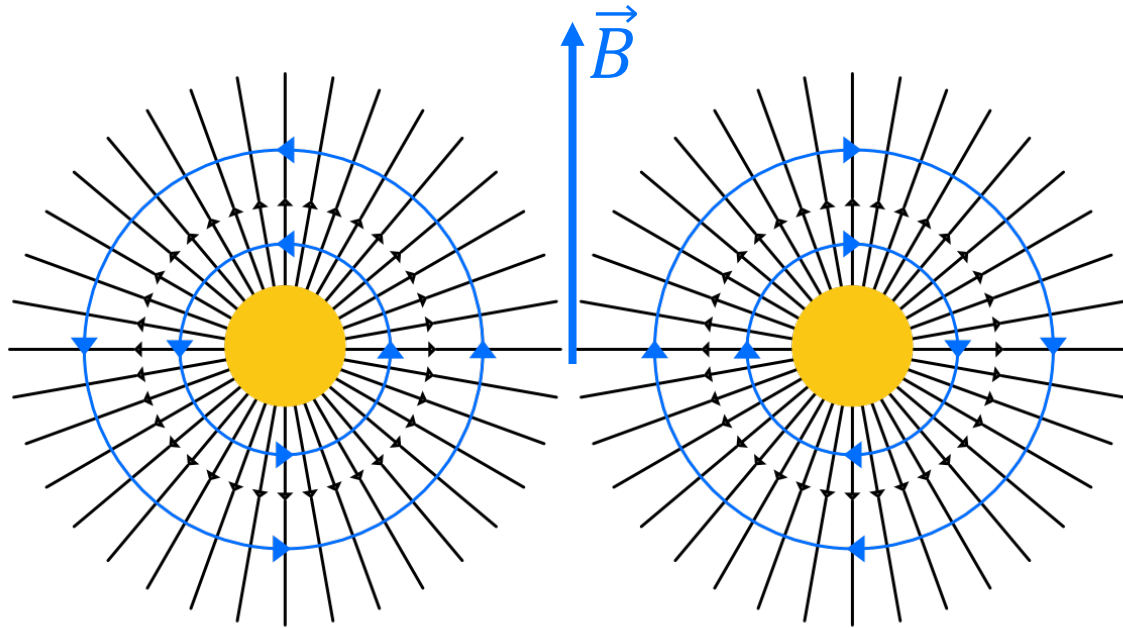
1. Many recent exciting developments in photo-processes
2. Experimental & theoretical advances
→ connection to initial EM field strength & distribution
3. First Earth-based evidence of vacuum birefringence :
 - Observed by STAR (6.7σ) via angular modulations in linear polarized $\gamma\gamma \rightarrow e^+e^-$ process
4. Experimental evidence that HIC produce the strongest magnetic fields in the Universe $\approx 10^{15}$ Tesla - over an extensive spatial distribution

A lot more work needed to further constrain magnetic field topology and to test for possible medium effects – Exciting opportunities lie ahead

Additional Slides

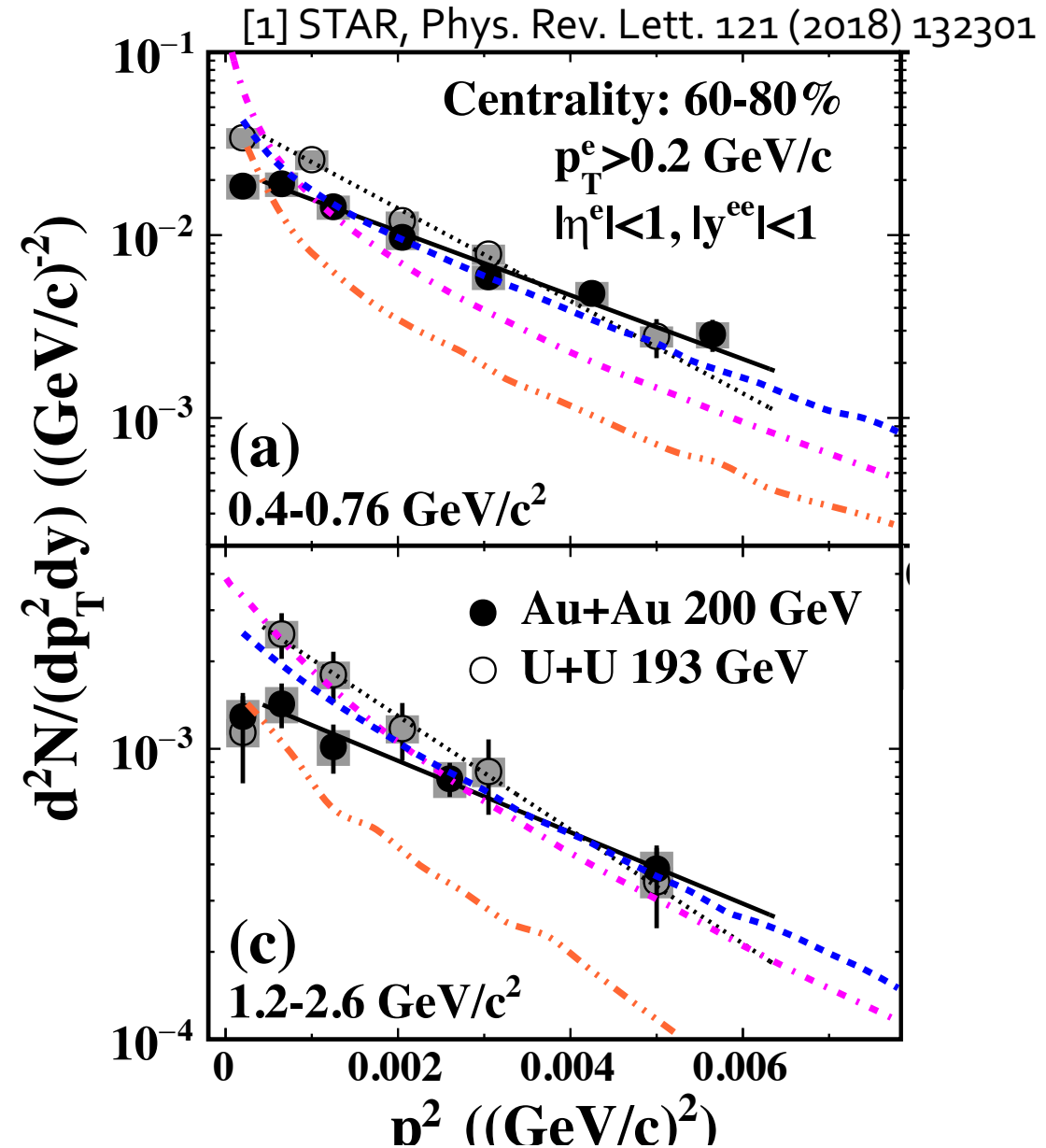
Long-lived Magnetic Field?

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$



Assumptions:

1. Used STARLight P_{\perp} Spectra
2. All e^{\pm} traverse 1 fm through $|B| \approx 10^{14} \text{ T}$ ($eBL \approx 30 \text{ MeV}/c$)

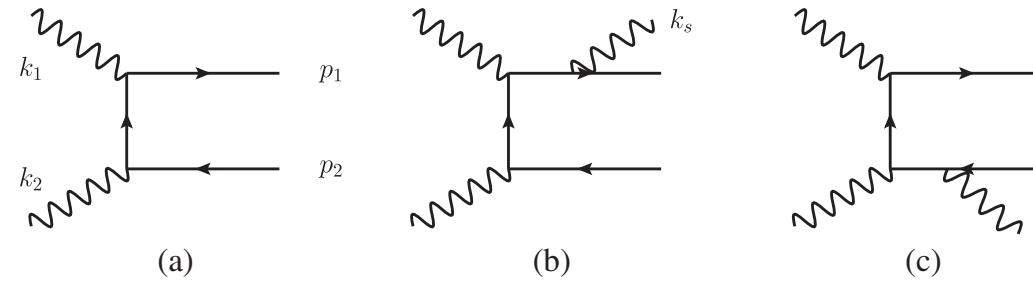
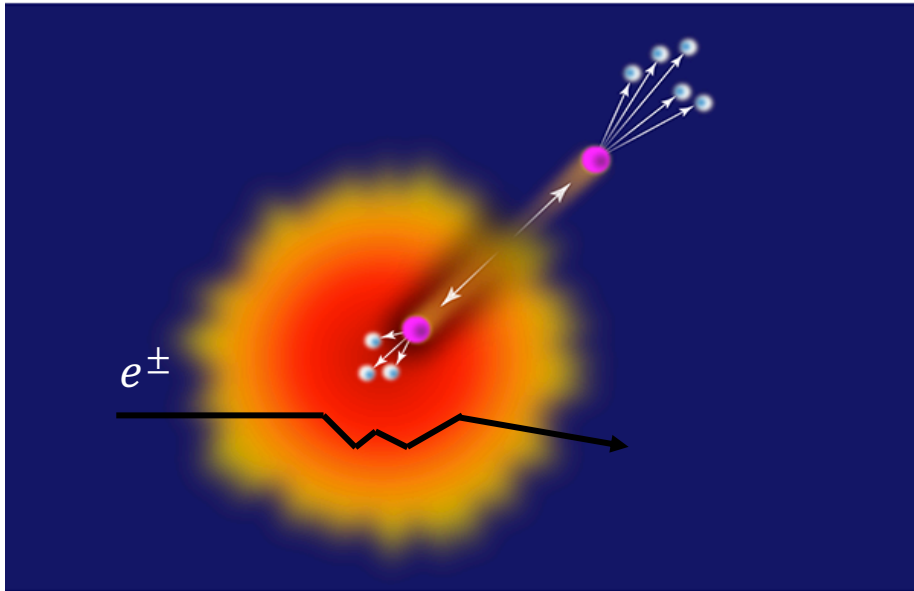


Coulomb Scattering through QGP

[1] S. R. Klein, et. al, Phys. Rev. Lett. 122, (2019), 132301

[2] ATLAS Phys. Rev. Lett. 121 (2018), 212301

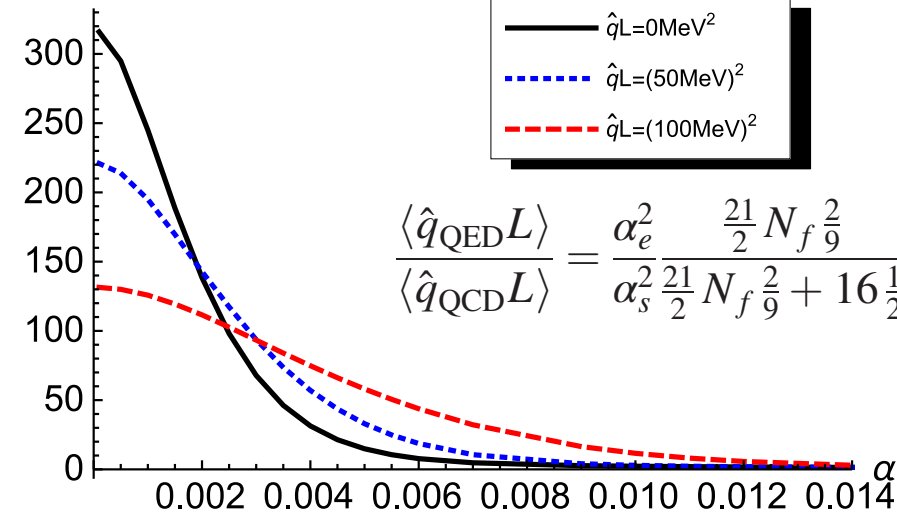
- Charged particles may scatter off charge centers in QGP, modifying primordial pair P_\perp



Assumptions:

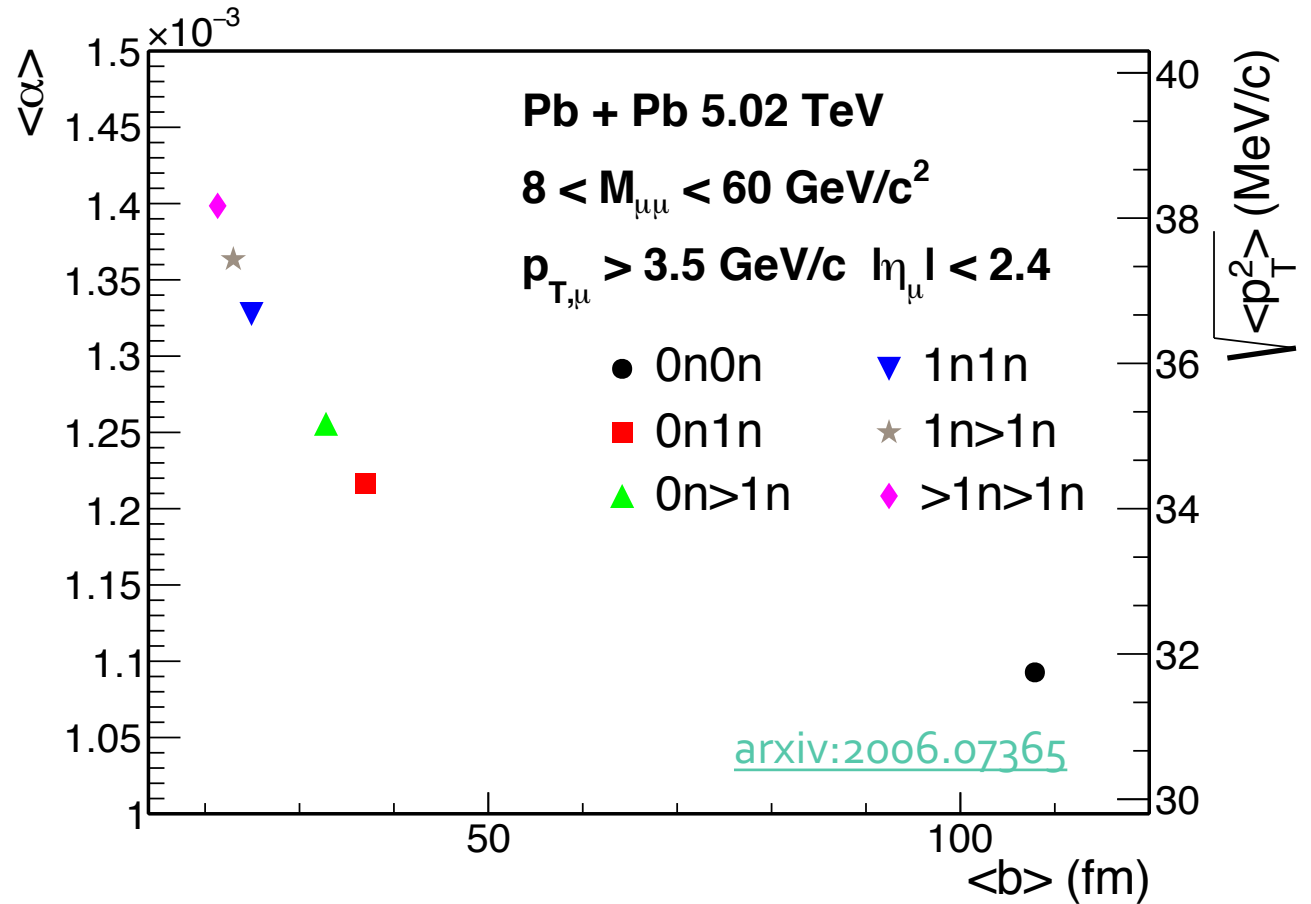
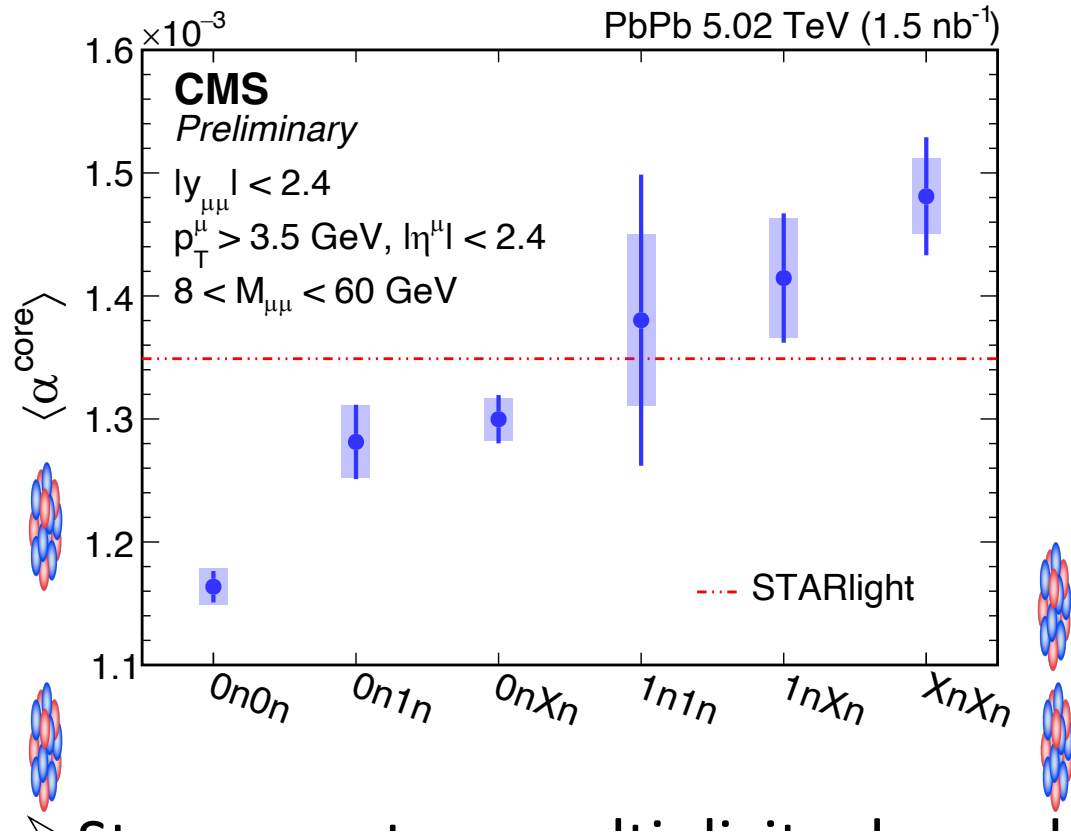
- Primordial distribution given by STARLight
- Daughters traverse medium

$(1/N)dN/d\alpha$

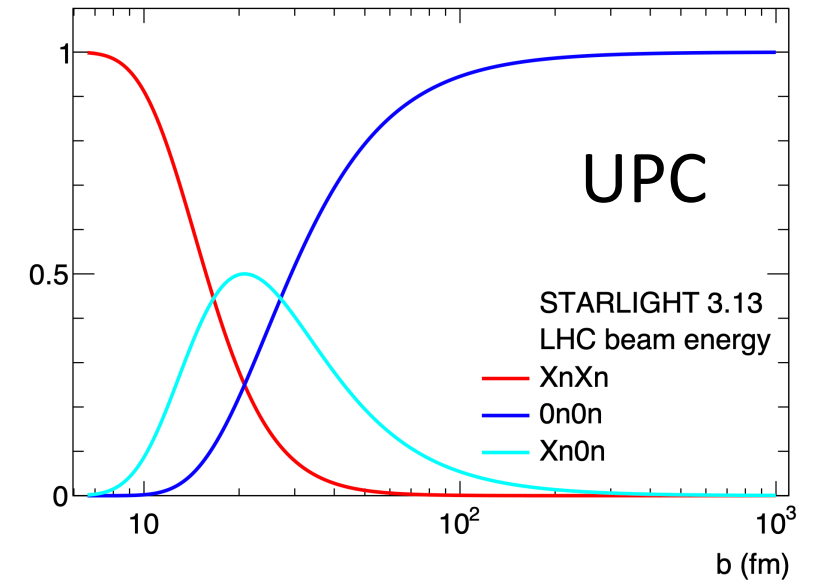
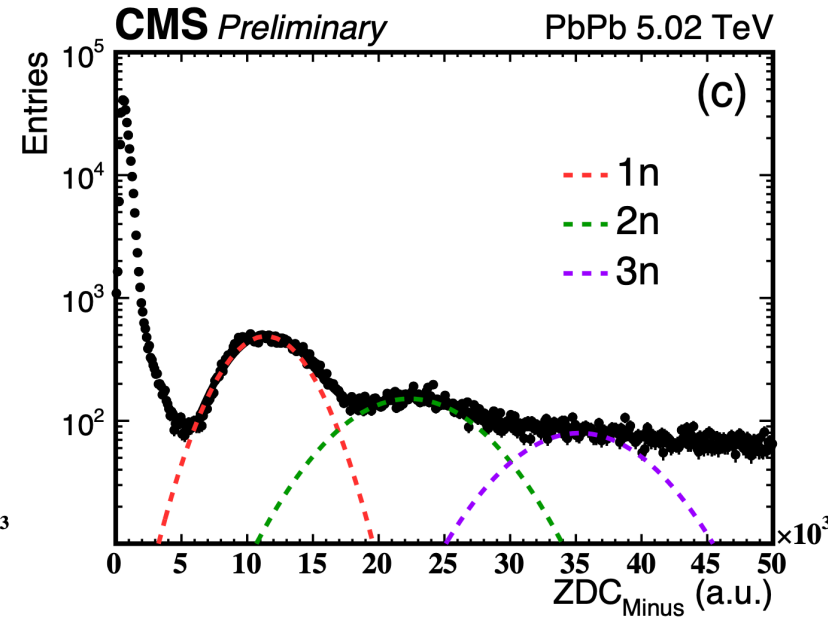
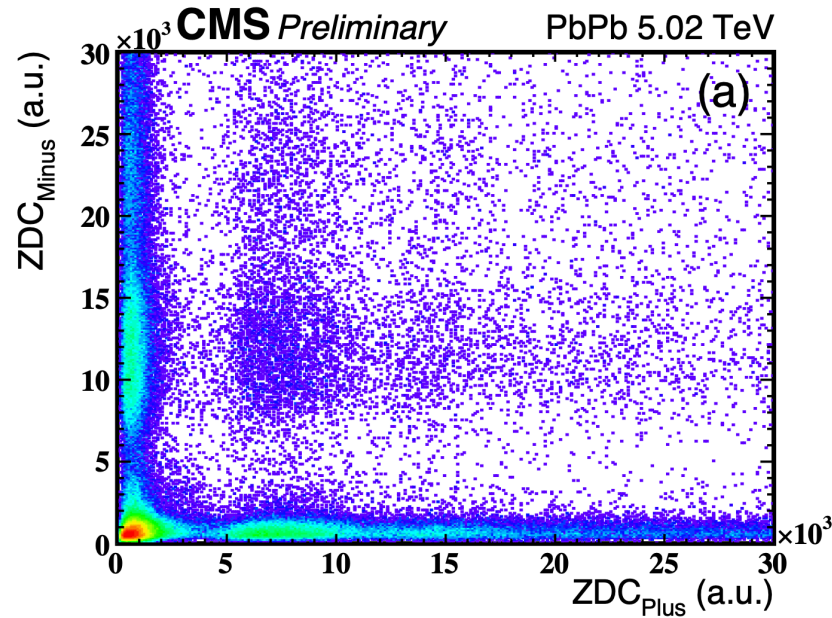


$$\frac{\langle \hat{q}_{\text{QED}} L \rangle}{\langle \hat{q}_{\text{QCD}} L \rangle} = \frac{\alpha_e^2 \frac{21}{2} N_f \frac{2}{9}}{\alpha_s^2 \frac{21}{2} N_f \frac{2}{9} + 16 \frac{1}{2}} = \frac{\alpha_e^2}{\alpha_s^2} \times \frac{7}{15},$$

QED Calculations & CMS Acoplanarity



Determine neutron multiplicity



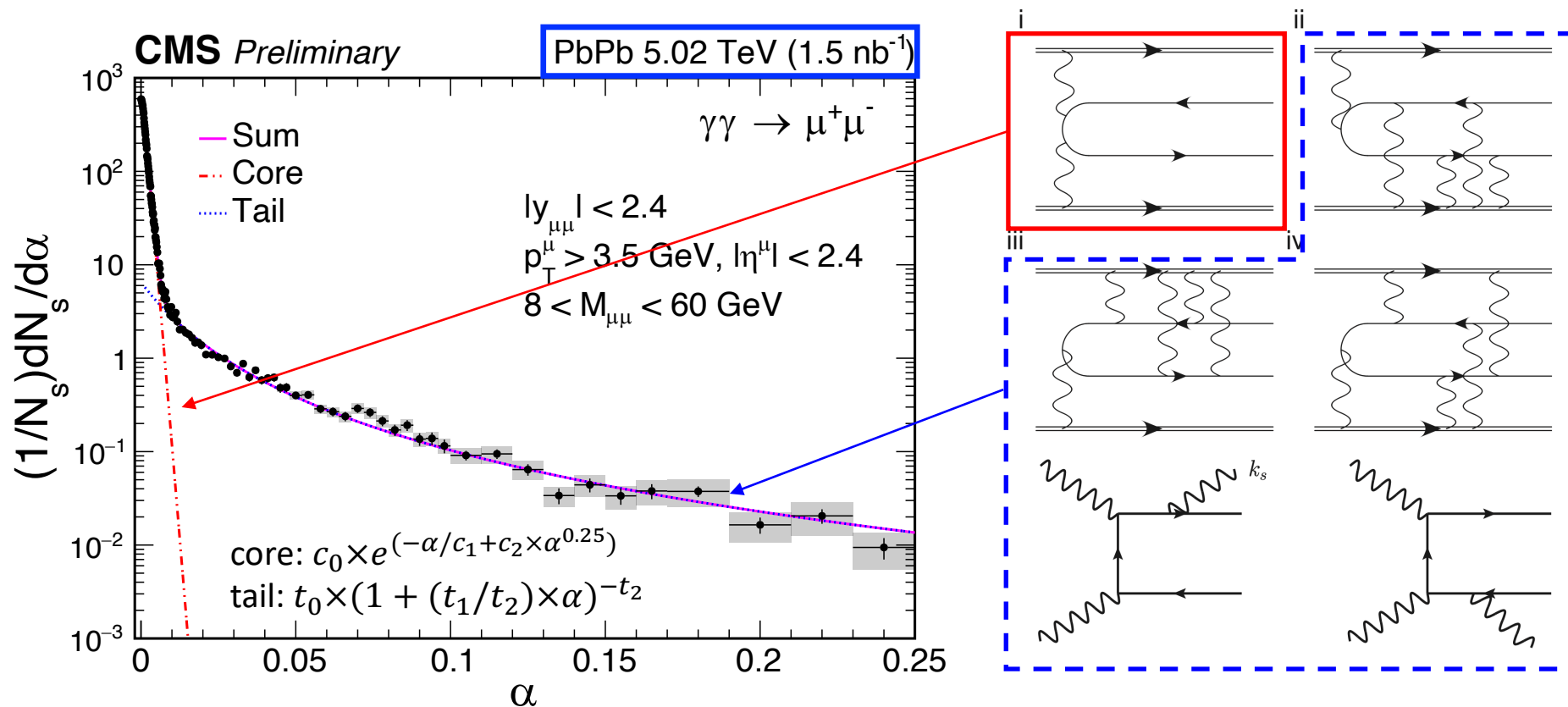
➤ Straight cut to disentangle neutrons

- $0n0n$, $0n1n$, $0nXn$, $1n1n$, $1nXn$, $XnXn$ ($X \geq 2$)

➤ Fit to estimate purity

- $0n$ and Xn : $\sim 100\%$
- $1n$: $\sim 93-95\%$

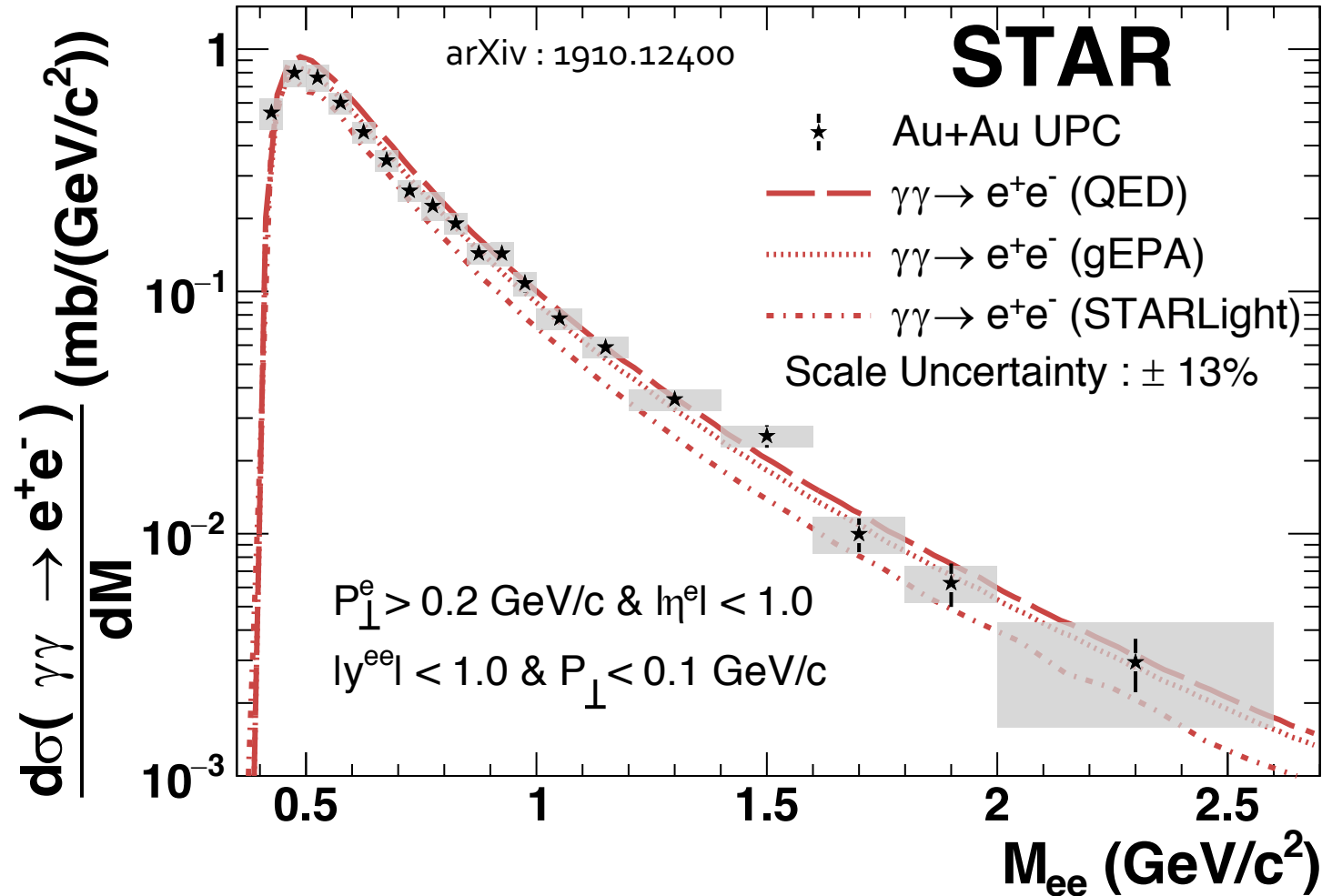
Leading order $\gamma\gamma \rightarrow \mu^+\mu^-$



➤ Decouple α spectrum:

- Data: $\langle \alpha^{\text{core}} \rangle = (1227 \pm 7 \text{ (stat.)} \pm 8 \text{ (syst.)}) \times 10^{-6}$
- STARlight: 1348×10^{-6}

Total $\gamma\gamma \rightarrow e^+e^-$ cross-section in STAR Acceptance



Pure QED $2 \rightarrow 2$ scattering :
 $d\sigma/dM \propto E^{-4} \approx M^{-4}$

No vector meson production
 \rightarrow Forbidden for real photons with
 helicity ± 1 (i.e. 0 is forbidden)

$\sigma(\gamma\gamma \rightarrow e^+e^-)$ in STAR Acceptance:

Data : 0.261 ± 0.004 (stat.) ± 0.013 (sys.)
 ± 0.034 (scale) mb

STARLight	gEPA	QED
0.22 mb	0.26 mb	0.29 mb

**Measurement of total cross
 section agrees with theory
 calculations at $\pm 1\sigma$ level**

STARLight: S. R. Klein, et. al. *Comput. Phys. Commun.* 212 (2017) 258

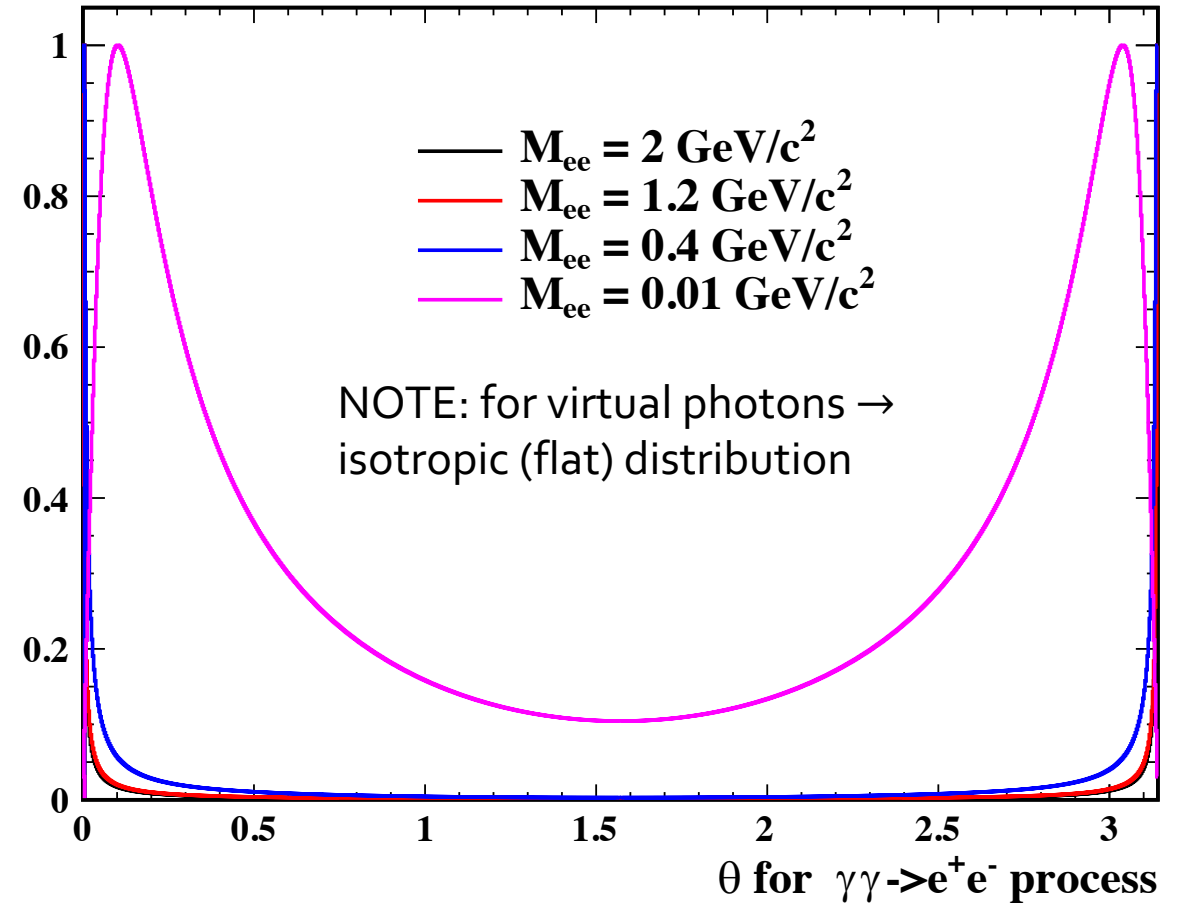
gEPA & QED : W. Zha, J.D.B., Z. Tang, Z. Xu arXiv:1812.02820 [nucl-th]

$d\sigma(\gamma\gamma \rightarrow e^+e^-)/d\cos\theta'$

$\gamma\gamma \rightarrow e^+e^-$: Individual e^+/e^- preferentially aligned along beam axis [1]:

$$G(\theta) = 2 + 4 \left(1 - \frac{4m^2}{W^2}\right) \frac{\left(1 - \frac{4m^2}{W^2}\right) \sin^2\theta \cos^2\theta + \frac{4m^2}{W^2}}{\left(1 - \left(1 - \frac{4m^2}{W^2}\right) \cos^2\theta\right)^2}$$

- Highly virtual photon interactions should have an isotropic distribution
- Measure θ' , the angle between the e^+ and the beam axis in the pair rest frame.



[1] S. Brodsky, T. Kinoshita and H. Terazawa, Phys. Rev. **D4**, 1532 (1971)
STARLight: S. R. Klein, et. al. *Comput. Phys. Commun.* 212 (2017) 258

$d\sigma(\gamma\gamma \rightarrow e^+e^-)/d\cos\theta'$

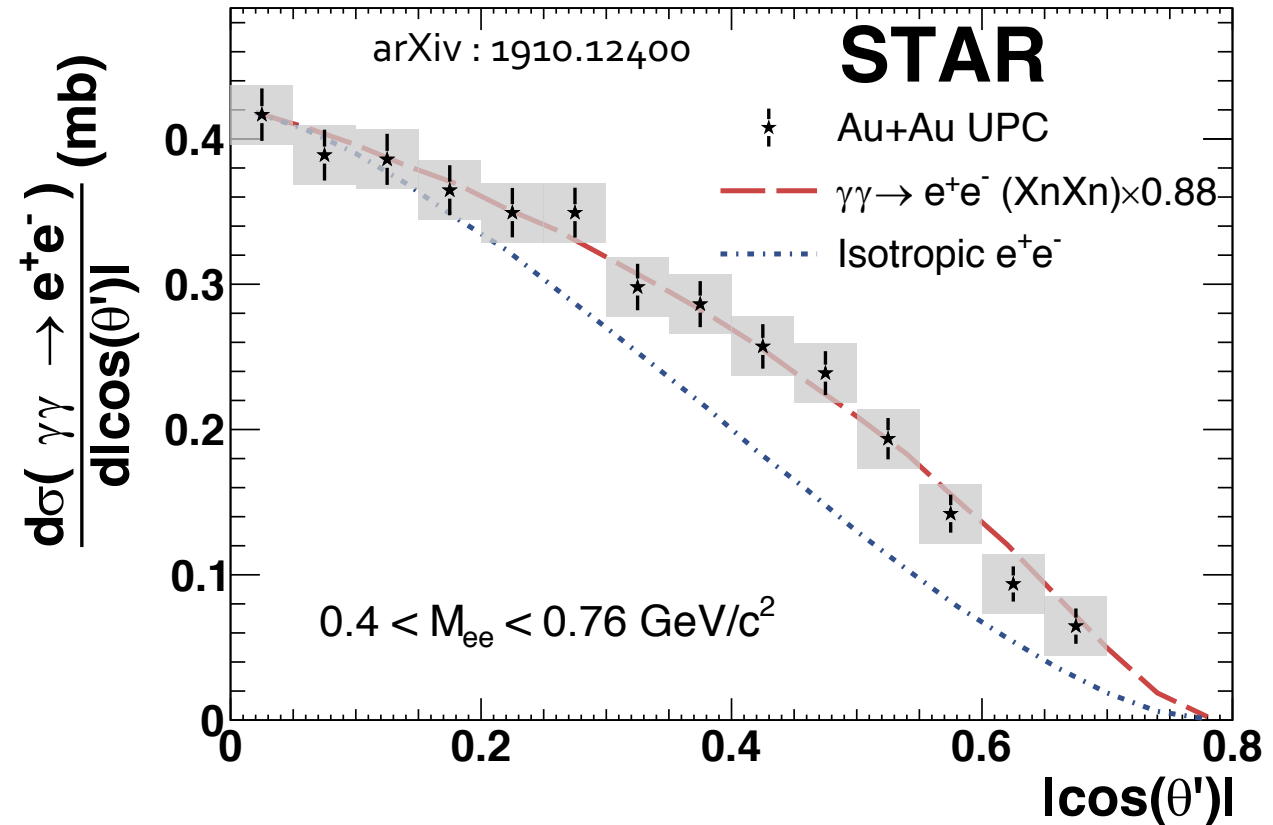
$\gamma\gamma \rightarrow e^+e^-$: Individual e^+/e^- preferentially aligned along beam axis [1]:

$$G(\theta) = 2 + 4 \left(1 - \frac{4m^2}{W^2} \right) \frac{\left(1 - \frac{4m^2}{W^2} \right) \sin^2\theta \cos^2\theta + \frac{4m^2}{W^2}}{\left(1 - \left(1 - \frac{4m^2}{W^2} \right) \cos^2\theta \right)^2}$$

- Highly virtual photon interactions should have an isotropic distribution
- Measure θ' , the angle between the e^+ and the beam axis in the pair rest frame.

⇒ Data are fully consistent with $G(\theta)$ distribution expected for $\gamma\gamma \rightarrow e^+e^-$

⇒ Measurably distinct from isotropic distribution



[1] S. Brodsky, T. Kinoshita and H. Terazawa, Phys. Rev. **D4**, 1532 (1971)
 STARLight: S. R. Klein, et. al. *Comput. Phys. Commun.* 212 (2017) 258

Outline of this talk

1. Introduction and Motivation
 - Motivation for direct measurement of electromagnetic fields
 - The extreme EM fields in heavy-ion collisions
2. Heavy ion collisions → QED under extreme conditions
 - Surprising results in peripheral heavy-ion collisions
 - Breit-Wheeler pair production & vacuum birefringence
3. A tool for precision mapping of the electromagnetic fields
4. Conclusions

